Modular system development by composing Petri nets on interfaces

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Joint work with

- Luca Bernardinello DISCo, University of Milano–Bicocca
- Carlo Ferigato JRC European Commission, Ispra
- Görkem Kılınç Phd student, Univ. Milano Bicocca
- Elisabetta Mangioni Phd, now CNR, Milano
- Elena Monticelli former Master Thesis student.
- Stefano Scacabarozzi former Master Thesis student.

Modular system development by composing Petri nets on interfaces

Outline

- Composing on interfaces, the intuition
- ② N-morphisms: abstraction and refinement
- Ocomposing on interfaces by N-morphisms
- Properties preserved/reflected
- **(5)** A new notion of morphisms: α -morphisms
- O Application to modular synthesis
- A case study
- Onclusions

$\mathsf{Section}\ 1$

Composing on interfaces, the intuition

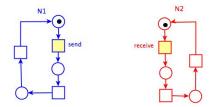
Composition operations for Petri nets

$$N=(P, T, F, M_0)$$

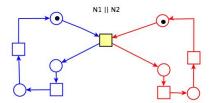
typical ways of composing nets

- synchronous
- asynchronous
- mixed

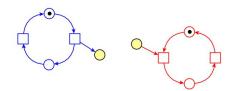
Synchronous Composition ||



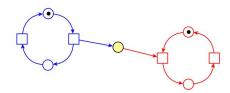
merging transitions (synchronization)



Asynchronous Composition



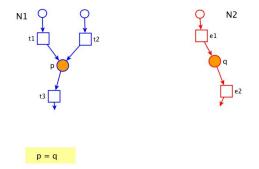
merging places (channels)



Composing on interfaces, the intuition...

Elementary net systems $N = (B, E, F, c_{in})$:

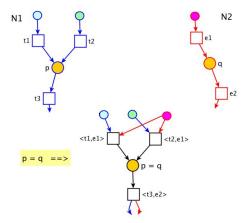
- B: conditions (boolean propositions) - E: events



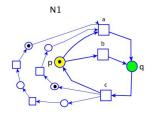
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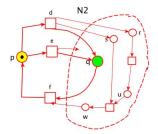
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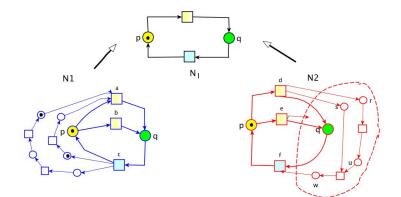
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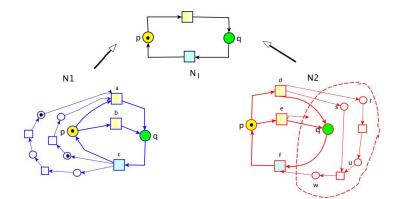


Composing on interfaces, the intuition...

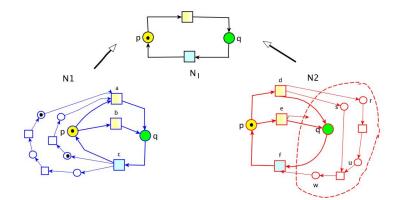








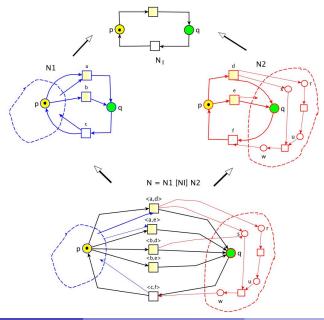
abstracting from details



abstracting from details

if q then $(s \land (r \lor u)) \lor w$

Composing Petri nets on interfaces



Section 2

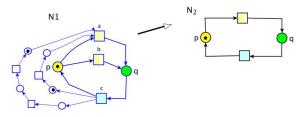
$\hat{N}\text{-}morphisms:$ abstraction and refinement

the origins

N-morphisms [Nielsen, Rozenberg, Thiagarajan '92]

(intuitively) they preserve behaviours, i.e.:

if $\phi : N_1 \rightarrow N_2$ is a *N*-morphism then N_2 is partially simulating N_1 .

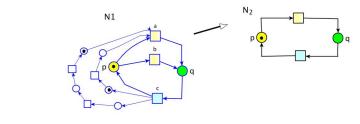


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Composing Petri nets on interfaces

¹L. Pomello, L. Bernardinello, Formal Tools for Modular System Development, in LNCS 3099, 77-96, Springer 2004.

²L.Bernardinello, E. Monticelli, L. Pomello, On preserving structural and behavioural properties by composing net systems on interfaces, Fundamenta Informaticae, Vol. 80, N.1-3, 31-47, 2007.

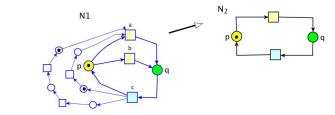


 $(\beta,\eta): N_1 \rightarrow N_2$ is an \hat{N} -morphism iff

 $\beta \subseteq B_1 \times B_2$ relation, $\eta : E_1 \to E_2$ partial surjective map :

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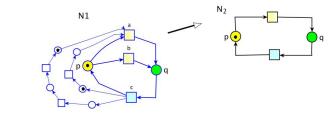
 $\beta \subseteq B_1 \times B_2$ relation, $\eta : E_1 \to E_2$ partial surjective map :

• $\beta^{-1}: B_2 \to B_1$ total injective map

•
$$\forall (b_1, b_2) \in \beta : b_1 \in c_{1, in} \Leftrightarrow b_2 \in c_{2, in}$$

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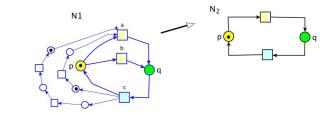
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• $\forall (b_1, b_2) \in \beta : b_1 \in c_{1,in} \Leftrightarrow b_2 \in c_{2,in}$
• $\eta(e_1) = e_2 \Rightarrow \beta(\bullet e_1) = \bullet e_2$ and $\beta(e_1 \bullet) = e_2^\circ$

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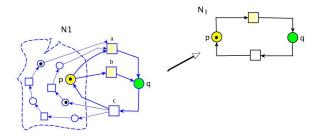
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• $\eta(e_1) = \bot \Rightarrow \beta(\bullet e_1) = \beta(e_1 \bullet) = \emptyset$

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N-morphisms for EN systems



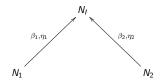
The counterimage of N_I , after T-simplification, is isomorphic to N_I .

N-morphisms: refinement /abstraction

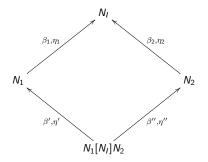
Section 3

Composing on interfaces by $\hat{N}\text{-morphisms}$

Composing two nets on an interface by $\hat{N}\text{-morphisms}$

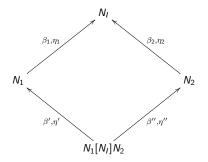


Composing two nets on an interface by $\hat{N}\text{-morphisms}$



 \hat{N} -morphisms dictate the identification (composition) of elements

Composing two nets on an interface by N-morphisms



 \hat{N} -morphisms dictate the identification (composition) of elements

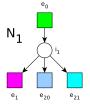


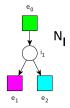
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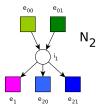
Composing Petri nets on interfaces

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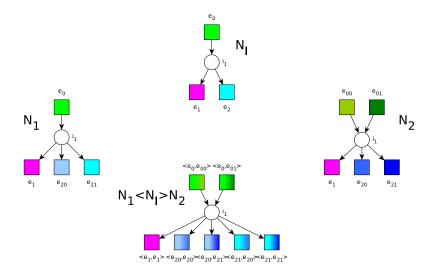
The composition: how to compose events



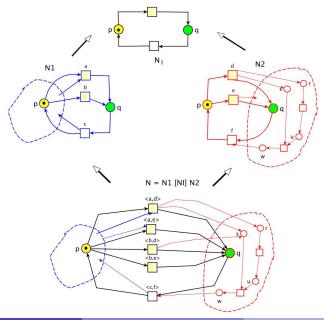




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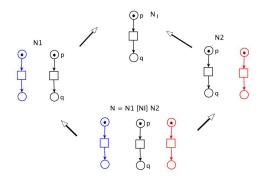


Composing on interfaces, by N-morphisms



Composition by \hat{N} -morphisms is **not** a Pullback

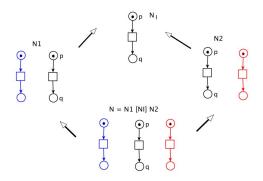
Example:



³M. A. Bednarczyk, L. Bernardinello, B. Caillaud, W. Pawlowski, L. Pomello, *Modular system development with pullbacks*, in ATPN2003, LNCS 2679, 140 - 160, Springer, 2003.

Composition by \hat{N} -morphisms is **not** a Pullback

Example:



A pullback composition has been defined on a bit different morphisms/ composition $^{\rm 3}$

³M. A. Bednarczyk, L. Bernardinello, B. Caillaud, W. Pawlowski, L. Pomello, *Modular system development with pullbacks*, in ATPN2003, LNCS 2679, 140 - 160, Springer, 2003.

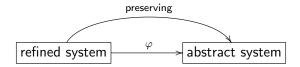
Section 4

Properties preserved/reflected

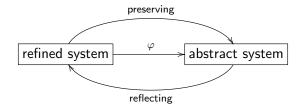
Preserving/reflecting properties



Preserving/reflecting properties



Preserving/reflecting properties



 \hat{N} -morphisms: properties preserved/reflected

 $(\beta,\eta): N_1 \rightarrow N_2$

• S-invariants are reflected:

if I_2 is an S-invariant of N_2 , then $I_1 = \beta^{-1}(I_2)$ is an S-invariant of N_1

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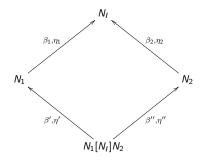
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- T-invariants are not reflected

Preserving properties



It is possible that N₁, N₁, N₂ are live, but N₁[N₁]N₂ is not live;
however, ...

reflecting sequences

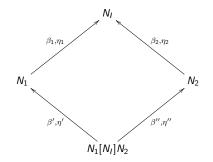
Definition

FS(N) firing sequences of N,

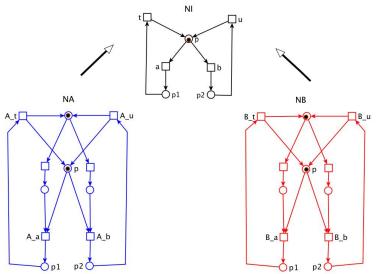
 $(\beta,\eta): N o N' \quad \hat{N}$ -morphism

N reflects the sequences of *N'* under (β, η) iff $\forall v \in FS(N'), \exists w \in FS(N)$ such that: $\hat{\eta}(w) = v$

Preserving properties

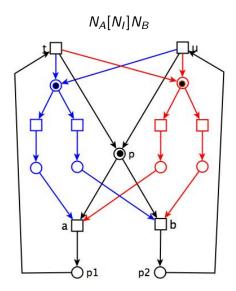


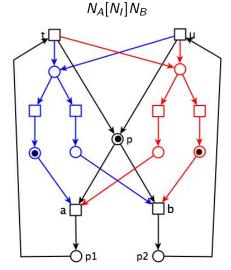
If N_1 and N_2 reflect the sequences of N_1 , respectively, then $N_1[N_1]N_2$ reflects the sequences of N_1 , N_2 and N_1 .



N_I , N_A and N_B are deadlock-free and even live.

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$N_A[N_I]N_B$ is dead

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if N' and N" are weakly bisimilar (N' \approx^{BIS} N")

then N' is deadlock-free iff N'' is deadlock-free

⁴R. Milner, A Calculus of Communicating Systems, 1980

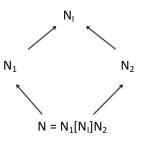
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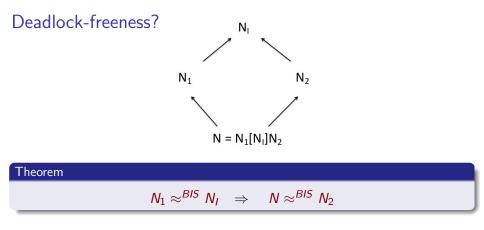
Remark

Weak Bisimulation is verified considering the reachability graphs.

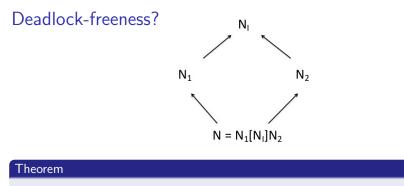
⁴R. Milner, A Calculus of Communicating Systems, 1980







if $N' \approx^{BIS} N$ " and N' is deadlock-free, then N" is deadlock-free



$$N_1 \approx^{BIS} N_I \Rightarrow N \approx^{BIS} N_2$$

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Section 5

Refinement and composition based on a *new* notion of morphisms: α -morphisms

Section 5

Refinement and composition based on a *new* notion of morphisms: α -morphisms

for Elementary Net systems, covered by sequential components

Refinement/abstraction and composition preserving/reflecting properties by considering behaviours, **only locally** Refinement/abstraction and composition preserving/reflecting properties by considering behaviours, **only locally**

Composition on Interfaces using α -morphisms: the idea 5 6

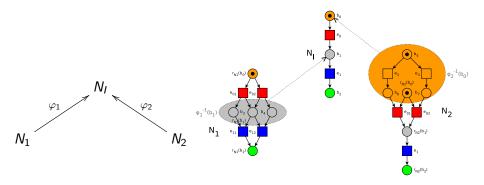


Nı

⁶Elisabetta Mangioni, Modularity for System Modelling and Analysis, PhD Thesis, Univ. Milano-Bicocca, 2013

⁵Luca Bernardinello, Elisabetta Mangioni and Lucia Pomello, Local State Refinement and Composition of Elementary Net Systems: An Approach Based on Morphisms, ToPNoC VIII, 2013

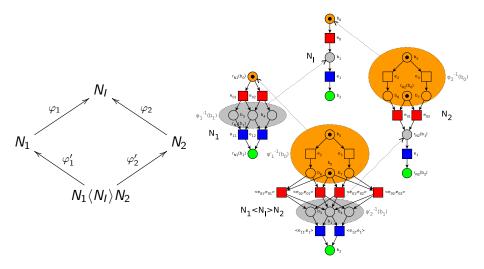
Composition on Interfaces using α -morphisms: the idea 5 6



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Composition on Interfaces using α -morphisms: the idea 5 6



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 - if an entering event to a bubble can fire then the bubble is empty
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- Sequential components are reflected
 - counter image of a sequential component is covered by sequential components

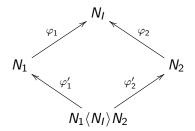
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 - 1. the initial marking of each bubble is at the start of the bubble itself
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 - 3. a "Local unfolding" condition

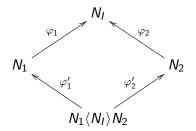
Composition based on α -morphisms, formal results



Proposition

• α -morphism: $N_1 \rightarrow N_I$ and 1 + 2 + 3 $\Rightarrow N_1$ is weakly bisimilar to N_I ;

Composition based on α -morphisms, formal results



Proposition

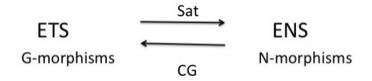
• α -morphism: $N_1 \rightarrow N_I$ and 1 + 2 + 3 $\Rightarrow N_1$ is weakly bisimilar to N_I ;

• α -morphism: $N_1 \rightarrow N_I$ and 1 + 2 + 3 and α -morphism: $N_2 \rightarrow N_I$ $\Rightarrow N_1 \langle N_I \rangle N_2$ is weakly bisimilar to N_2 . Section 6

Application to modular synthesis (on the basis of \hat{N} -morphisms)

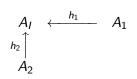
Synthesis

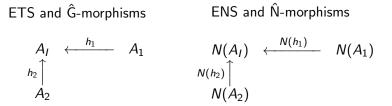
A = (S, E, T)Elementary Transition Systems N = (B, E, F)Elementary Nets Systems

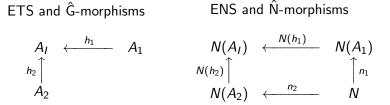


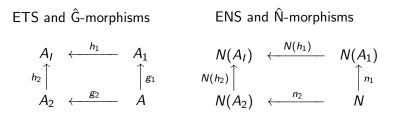
[Nielsen, Rozenberg, Thiagarajan '92]

ETS and $\hat{\mathsf{G}}\text{-morphisms}$









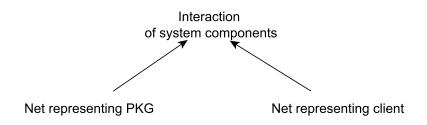
CG(N) is isomorphic to A

[Bernardinello, Ferigato, Pomello 02]

Section 7

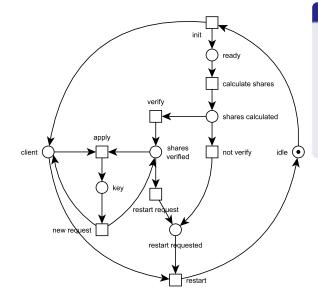
A case study Modeling and Analyzing a Distributed Private Key Generation Protocol

Modeling Distributed Private Key Generation Protocol 7



⁷L. Bernardinello, G. Kılınç, E. Mangioni, L. Pomello, *Modeling Distributed Private Key Generation by Composing Petri Nets*, Int. Workshop PNSE'13, 2013 (to appear in TopNoC, Springer).

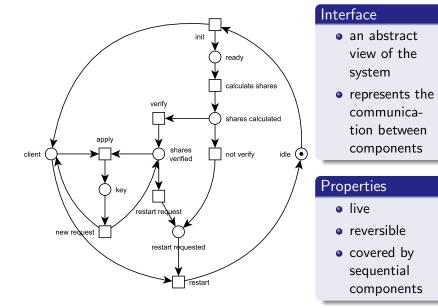
Interface Net, N_I



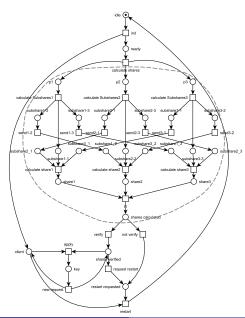
Interface

- an abstract view of the system
- represents the communication between components

Interface Net, N_I



Net Representing PKG, N_{PKG}

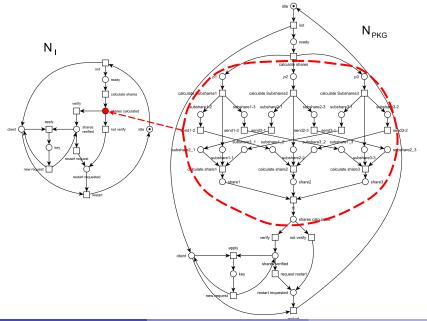


Properties

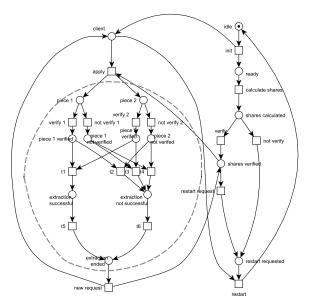
live

- reversible
- covered by sequential components

$\alpha\text{-morphism}$



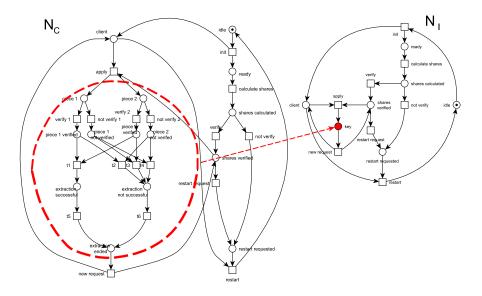
Net Representing the Client, N_C



Properties

live

- reversible
- covered by sequential components



- There is an α -morphism both from N_{PKG} to N_I and from N_C to N_I .
- Additional requirements are satisfied.

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➡

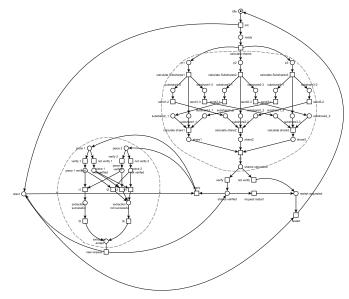
- Reflection of reachable markings property is held.
- Weakly bisimulation property is held.
 - N_{PKG} is weakly bisimilar to N_I .
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- Weakly bisimulation property is held.
 - N_{PKG} is weakly bisimilar to N_I .
 - N_C is weakly bisimilar to N_I .
 - Consequently, $N_{PKG} \langle N_I \rangle N_C$ is weakly bisimilar to N_I .

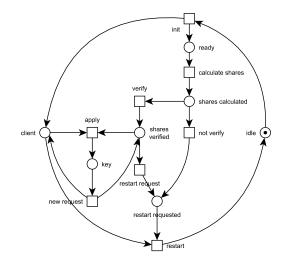
Analysis on the Composed Net . . .



Ex: A property to be analyzed: "Shares cannot be verified while distribution or extraction process is continuing"

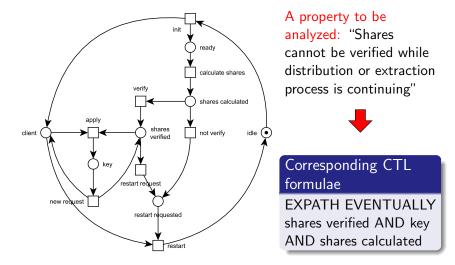
Analysis on the Composed Net can be done directly on the Interface

even without computing the Composed Net



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Section 8

Remarks and Conclusions

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- an other notion of morphisms for marked graphs has been studied (paper just submitted to PNSE 2014)

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Future?

- Define and study α-morphisms and the other just defined notion for more general classes (e.g.: P/T nets, high level nets, Coloured nets,...)
- Morphisms and compositionality on Petri Hypernets or on Nested nets

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THANK YOU !

Спасибо большое !

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Arrivederci!...

