

On Negotiation as Concurrency Primitive

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On Negotiation as Concurrency Primitive I: arbitrary / **weakly deterministic** /deterministic cyclic / **acyclic** Negotiations

[CONCUR 2013]

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On Negotiation as Concurrency Primitive II: arbitrary / weakly deterministic / **deterministic** **cyclic** / acyclic Negotiations

[FOSSACS 2014]

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Negotiation Programs

[unpublished]

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(Multiparty) negotiation

Negotiation as a metaphor for distributed problem solving

R Davis, [RG Smith](#) - Artificial intelligence, 1983 - Elsevier

[Automated negotiation: prospects, methods and challenges](#)

soton.ac.

[QR](#) [NR Jennings](#), [P Faratin](#), [AR Lomuscio](#)... - ... and **Negotiation**, 2001 - Springer

[flig](#) **AUTOMATED NEGOTIATION: PROSPECTS, METHODS AND CHALLENGES** Group e
Decision ted ...
TF and **Negotiation** 10: 199–215, 2001 © 2001 Kluwer Academic Publishers. Printed in the
Ab Netherlands
SD

[\[book\]](#) Rules of encounter: designing conventions for **automated negotiation** among computers

[JS Rosenschein](#) - 1994 - [books.google.com](#)

Rules of Encounter applies the general approach and the mathematical tools of game theory in a formal analysis of rules (or protocols) governing the high-level behavior of interacting heterogeneous computer systems. It describes a theory of high-level protocol design that ...

[Cited by 1760](#) [Related articles](#) [All 8 versions](#) [Import into BibTeX](#) [More](#) ▾

negotiation-based protocols, meta-data, information dissemination 1. Introduction ...

[Cited by 1035](#) [Related articles](#) [All 22 versions](#) [Import into BibTeX](#) [More](#) ▾

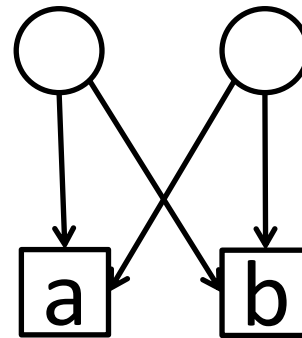
Negotiation as concurrency primitive

- Concurrency theory point of view:

Negotiation = synchronized choice

- CSP: $(aP_1 + bP_2) \mid \{a, b\} \mid (aQ_1 + bQ_2)$

- Petri nets:



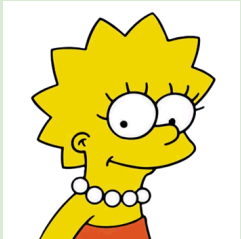
- **Negotiations:** a net-like concurrency model with negotiation as primitive.

The Father-Daughter-Mother Negotiation

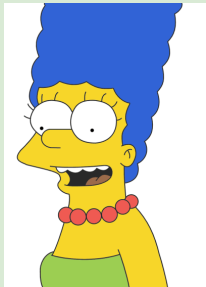
Agents



Father



Daughter

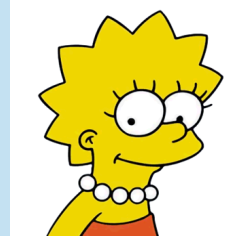


Mother

Initial states



11:00 pm

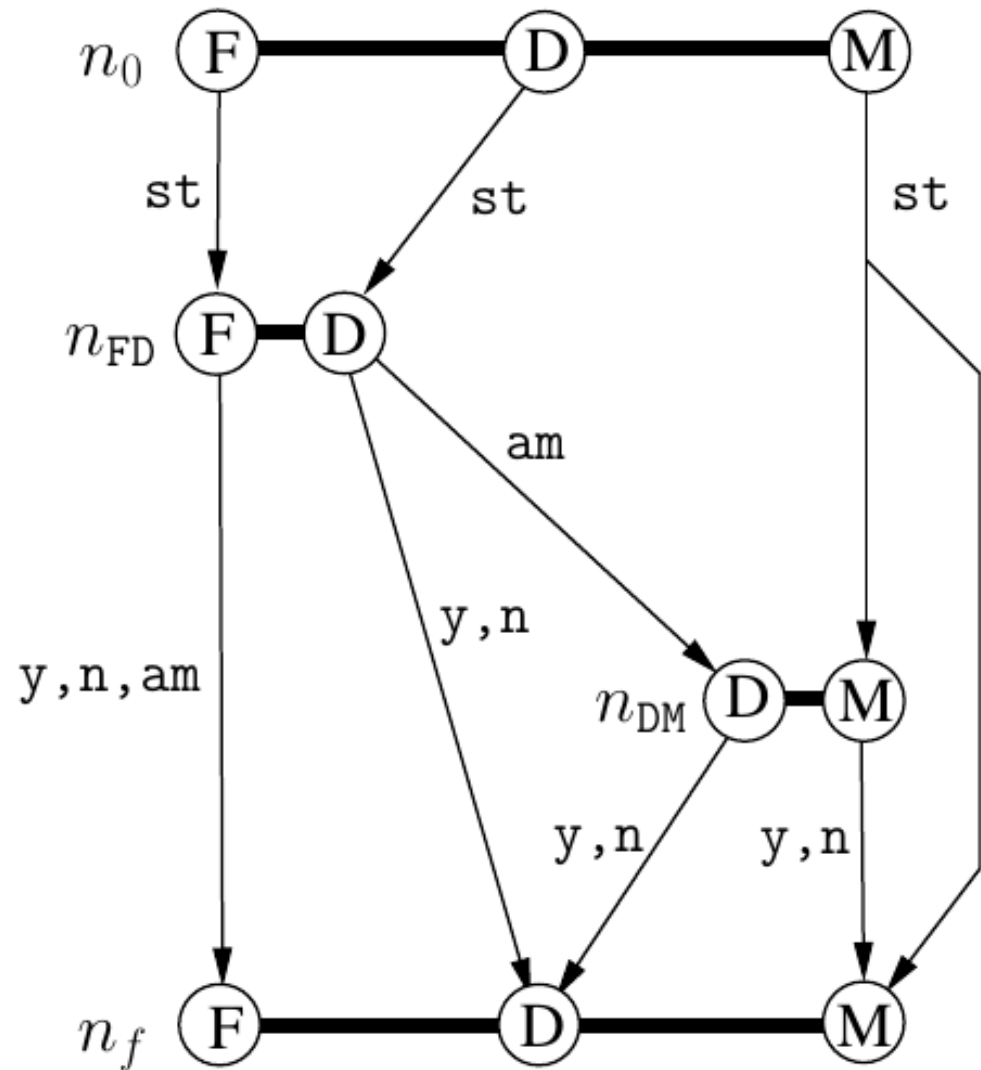


2:00 am



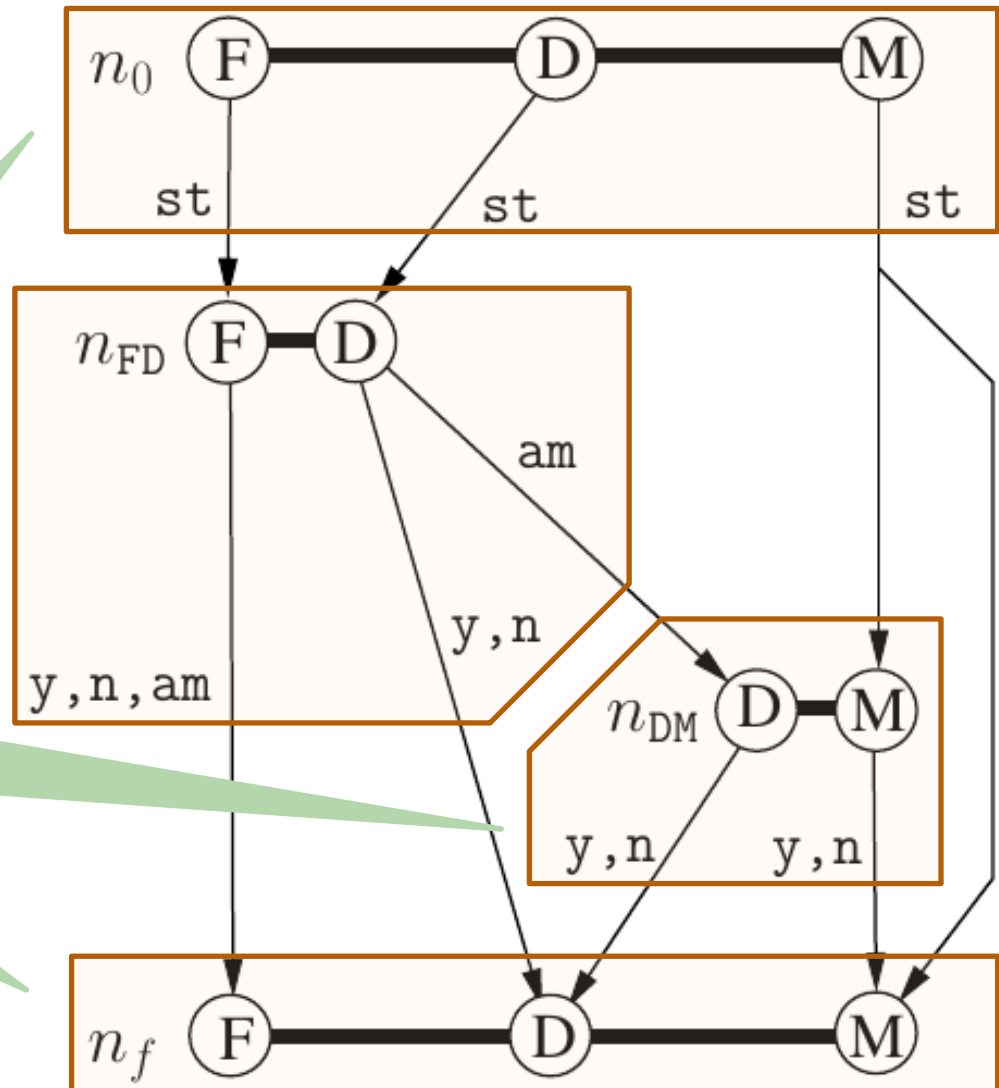
10:00 pm

The Father-Daughter-Mother Negotiation

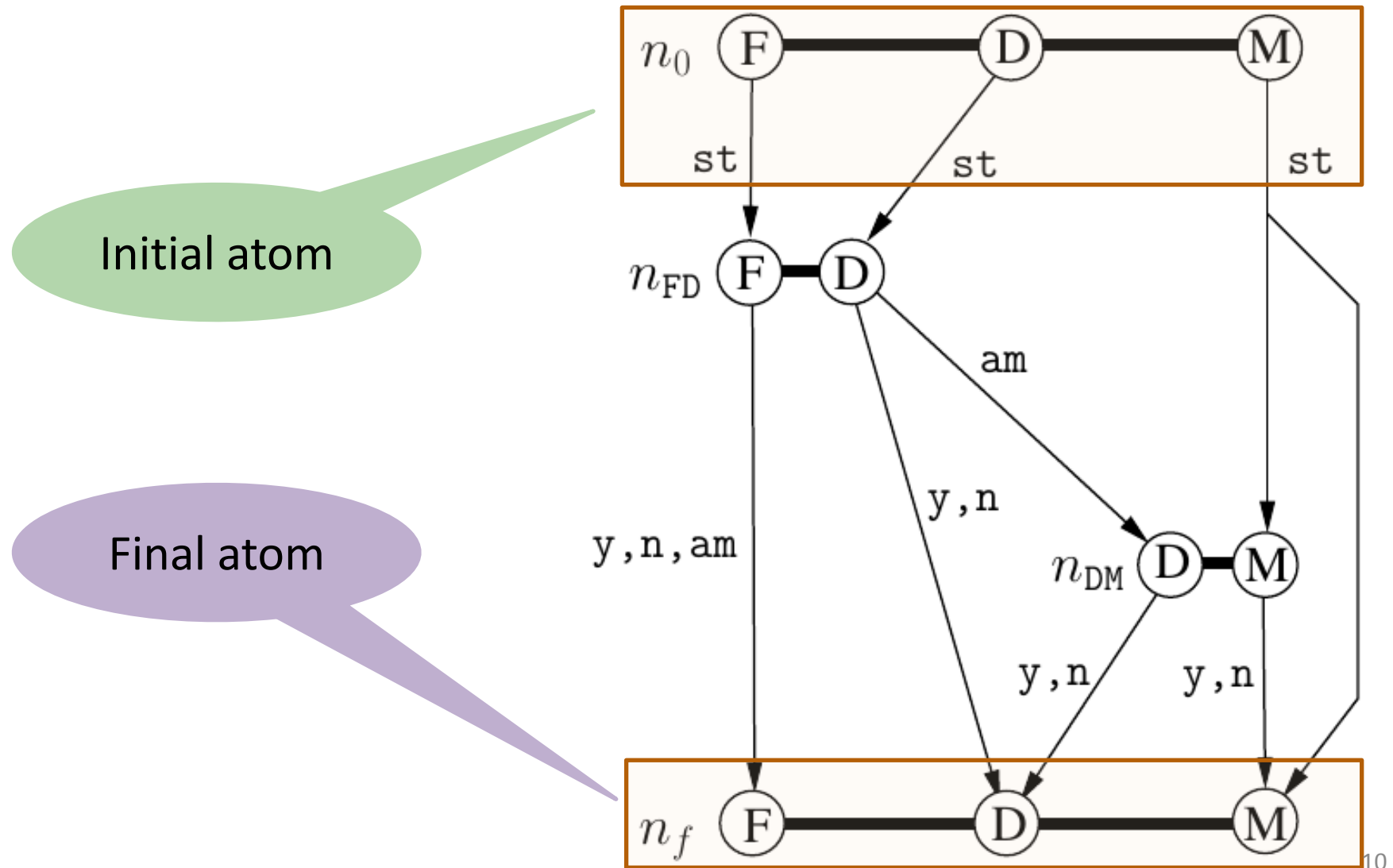


The Father-Daughter-Mother Negotiation

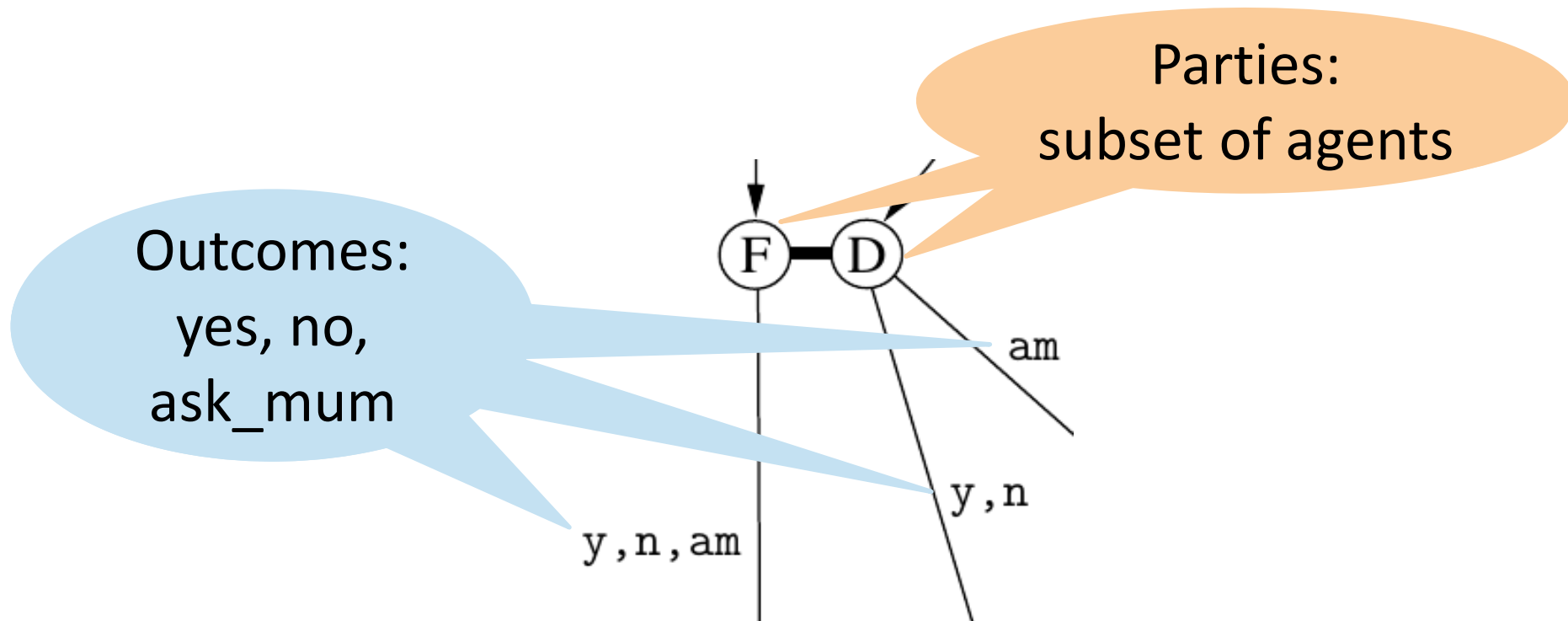
Atomic
negotiations
(atoms)



The Father-Daughter-Mother Negotiation



An atomic negotiation



State transformers (one per outcome):

$$T_{am}(tf, td) = (tf, td)$$

$$T_y(tf, td) = \{(t, t) \mid tf \leq t \leq td\}$$

(sometimes we identify a and T_a)

Semantics



11:00

2:00

10:00

11:00

2:00

10:00

12:00

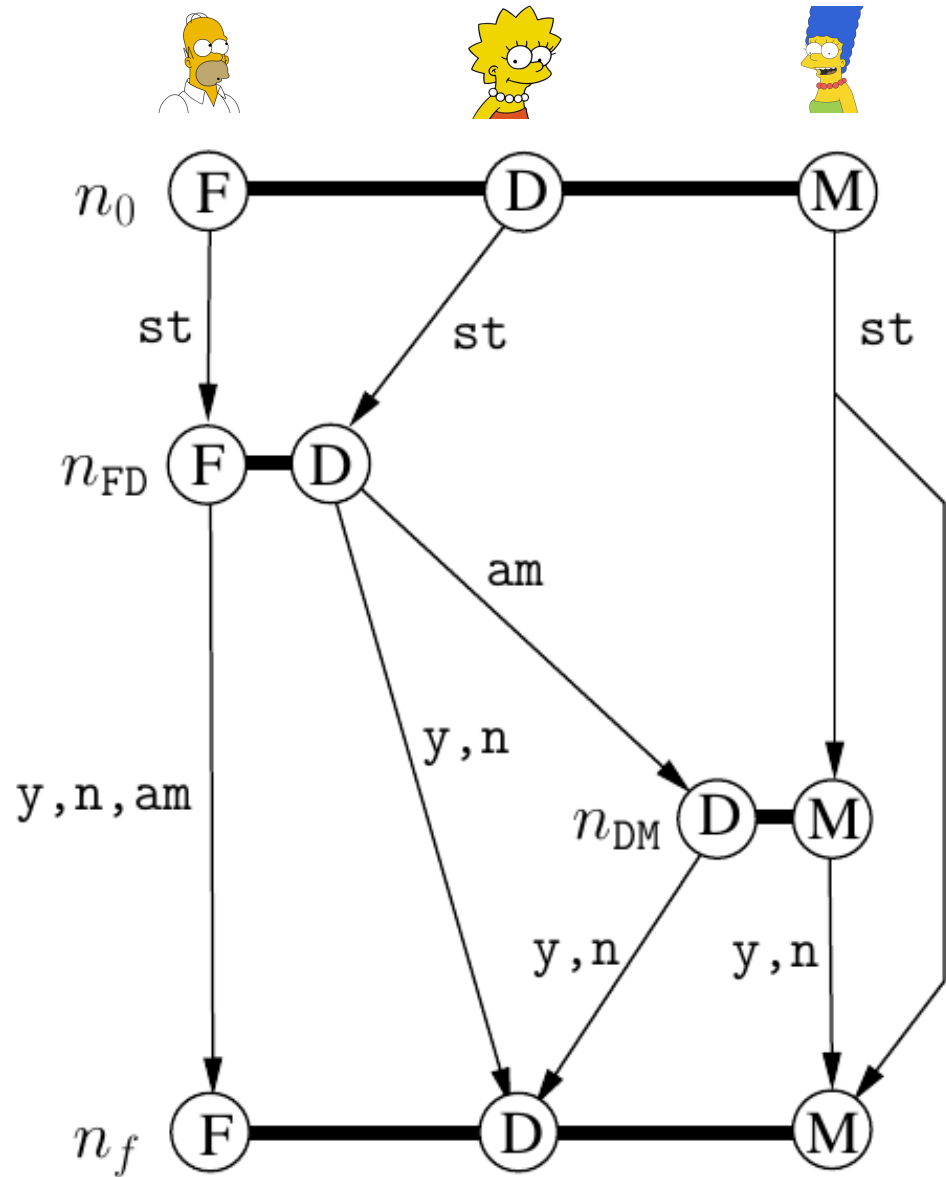
12:00

10:00

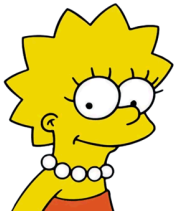
12:00

12:00

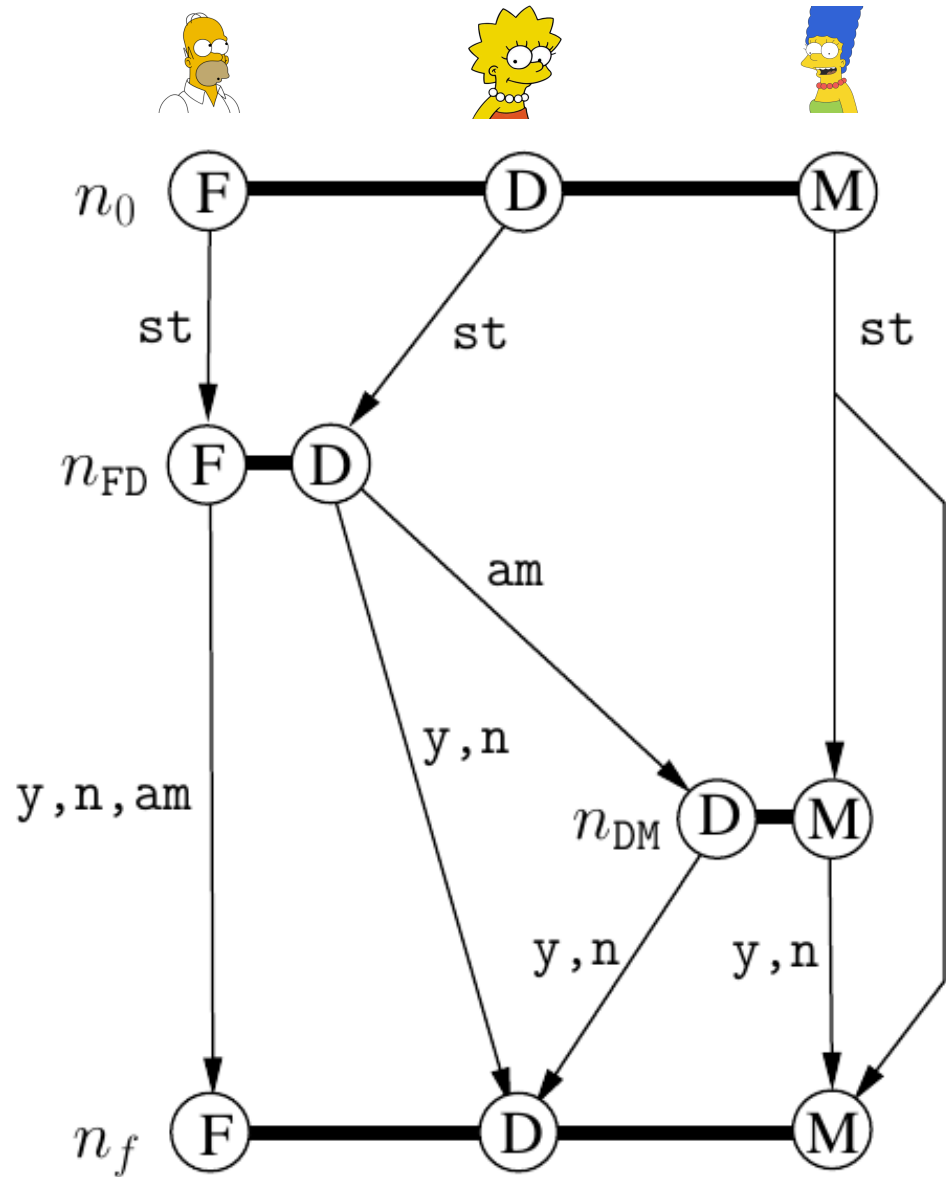
12:00



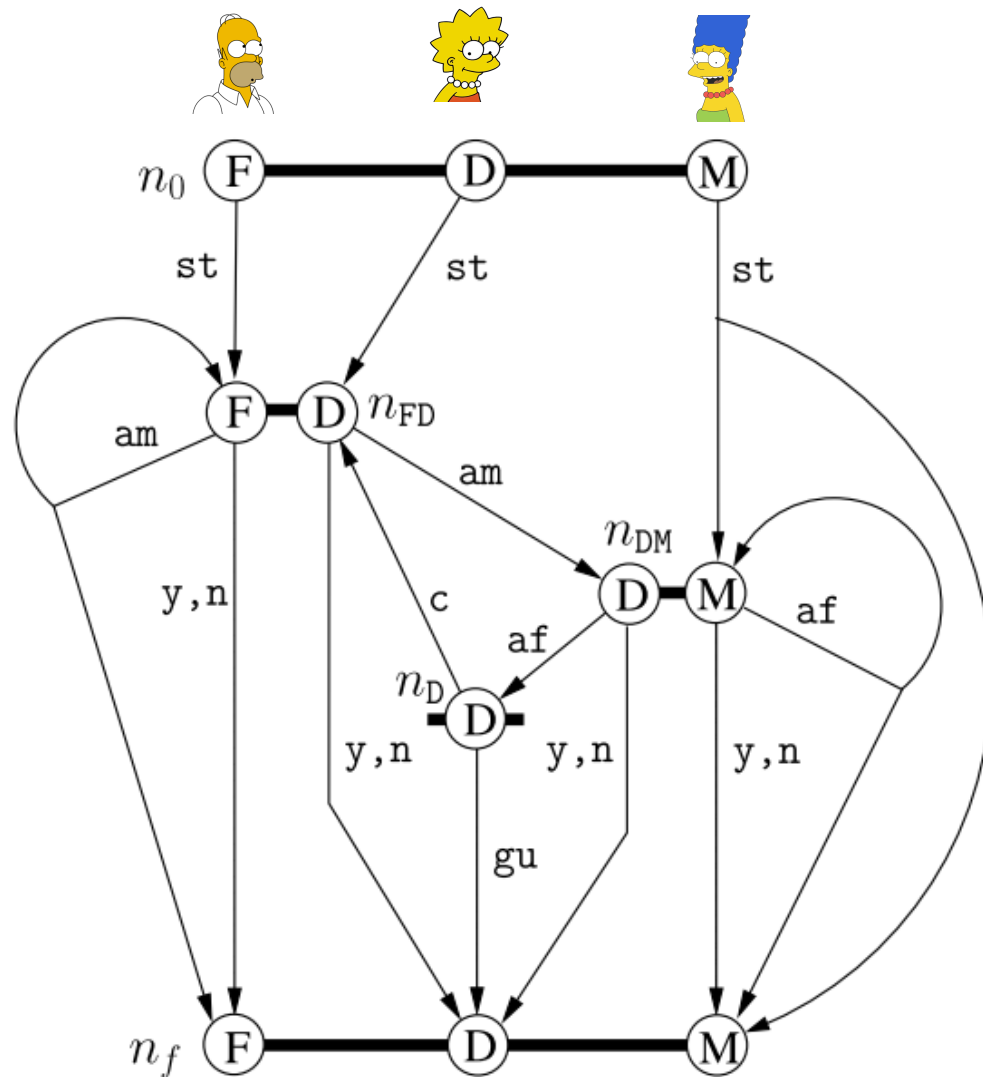
Semantics



11:00	2:00	10:00
11:00	2:00	10:00
11:00	2:00	10:00
11:00	Angry!	Angry!
Beer!	Angry!	Angry!

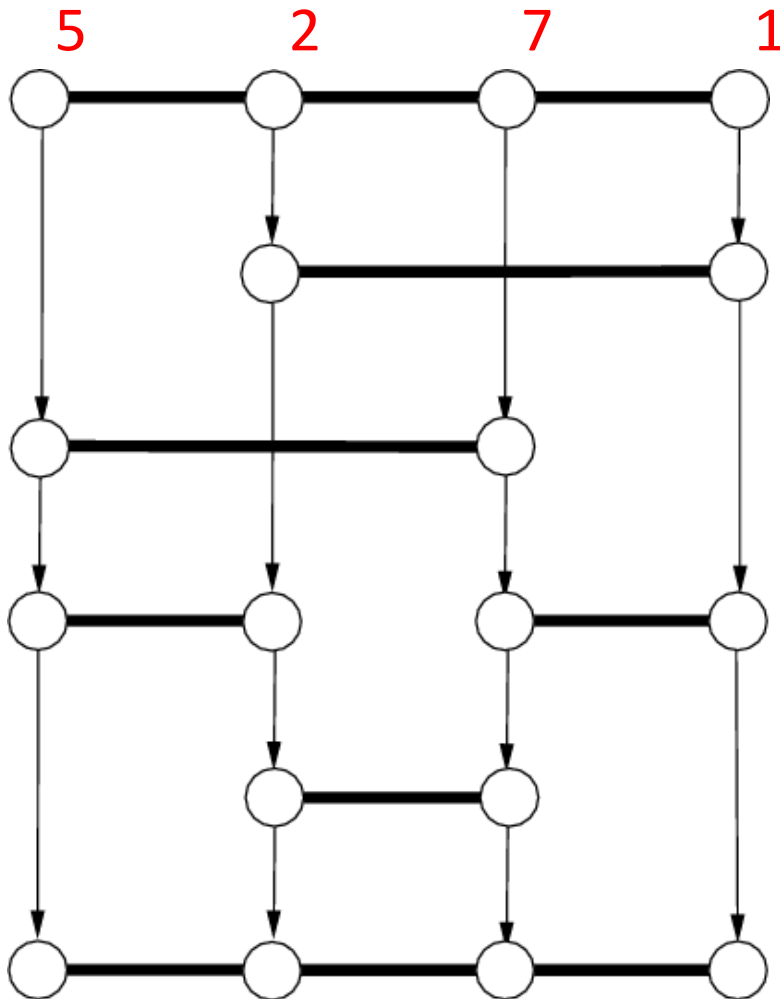


The Ping-Pong Negotiation



Negotiations as Parallel Computation Model.

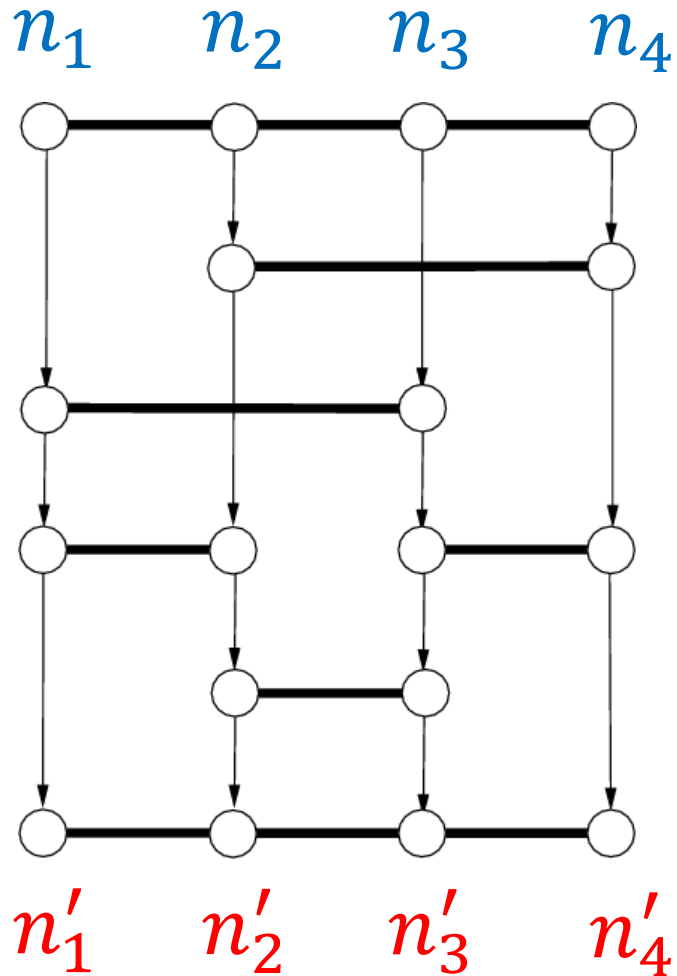
An Example: Sorting four integers



- Four agents.
- Internal states: integers.
- Transformer of internal atom: swap integers if not in ascending order.

$$T(x, y) = \text{if } y < x \text{ then } (y, x) \\ \text{else } (x, y)$$

Analysis of the sorting negotiation



Sorting negotiation correct if

- sound, and
- summary consists of all pairs

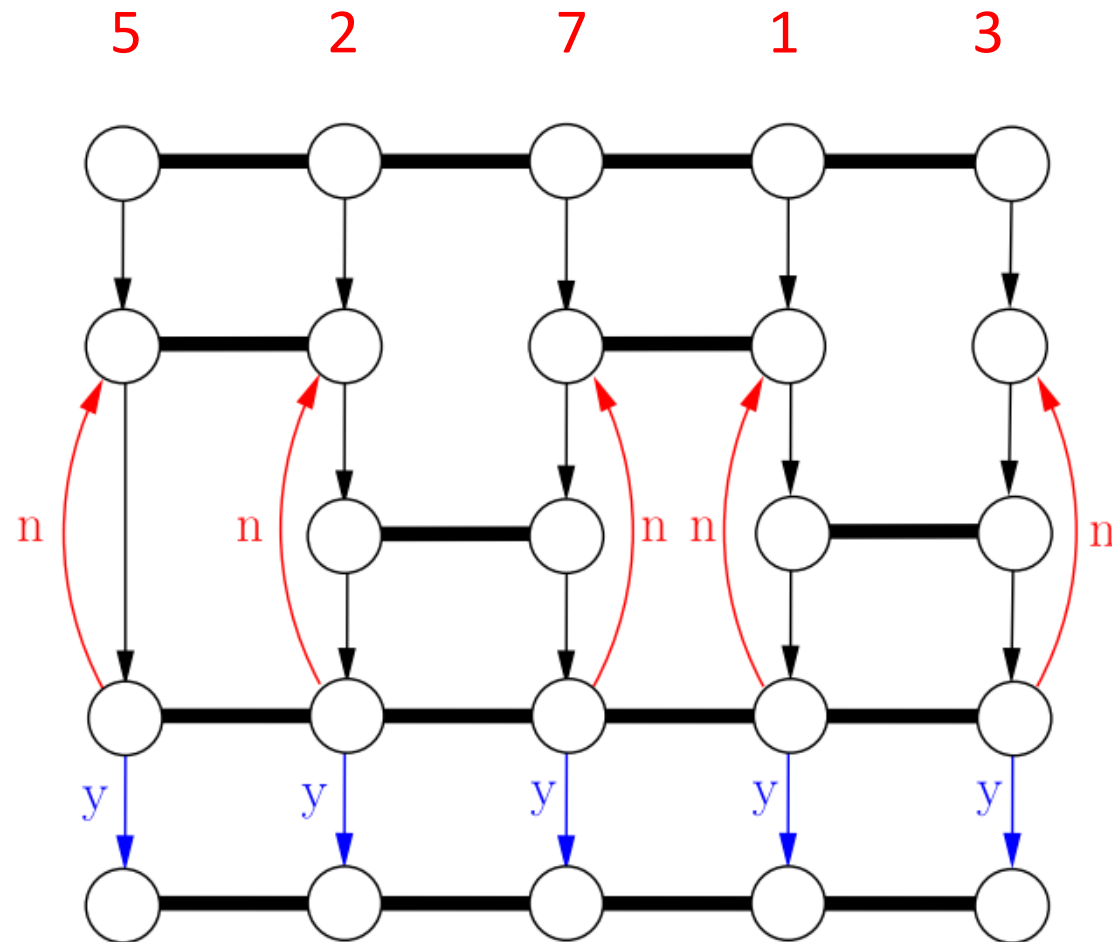
((n_1, n_2, n_3, n_4) , (n'_1, n'_2, n'_3, n'_4))

s. t. $n'_1 n'_2 n'_3 n'_4$ is a permutation of

$n_1 n_2 n_3 n_4$ and $n'_1 \leq n'_2 \leq n'_3 \leq n'_4$

Negotiations as Parallel Computation Model.

Parallel Bubblesort

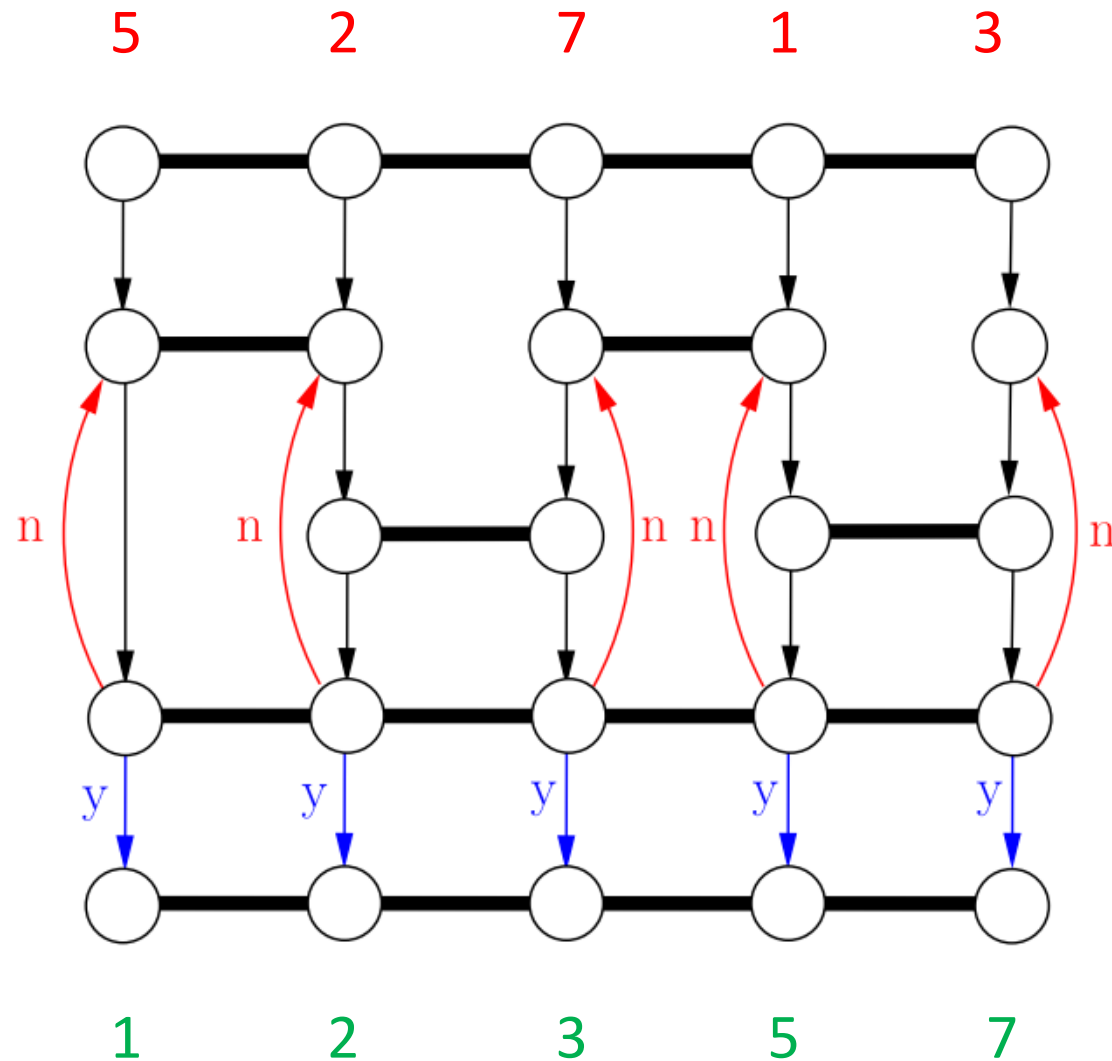


- Five agents.
- Internal states: integers.
- Transformer of internal binary atom: swap integers if not in ascending order.

$T(x, y) = \text{if } y < x$
then (y, x)
else (x, y)

Negotiations as Parallel Computation Model.

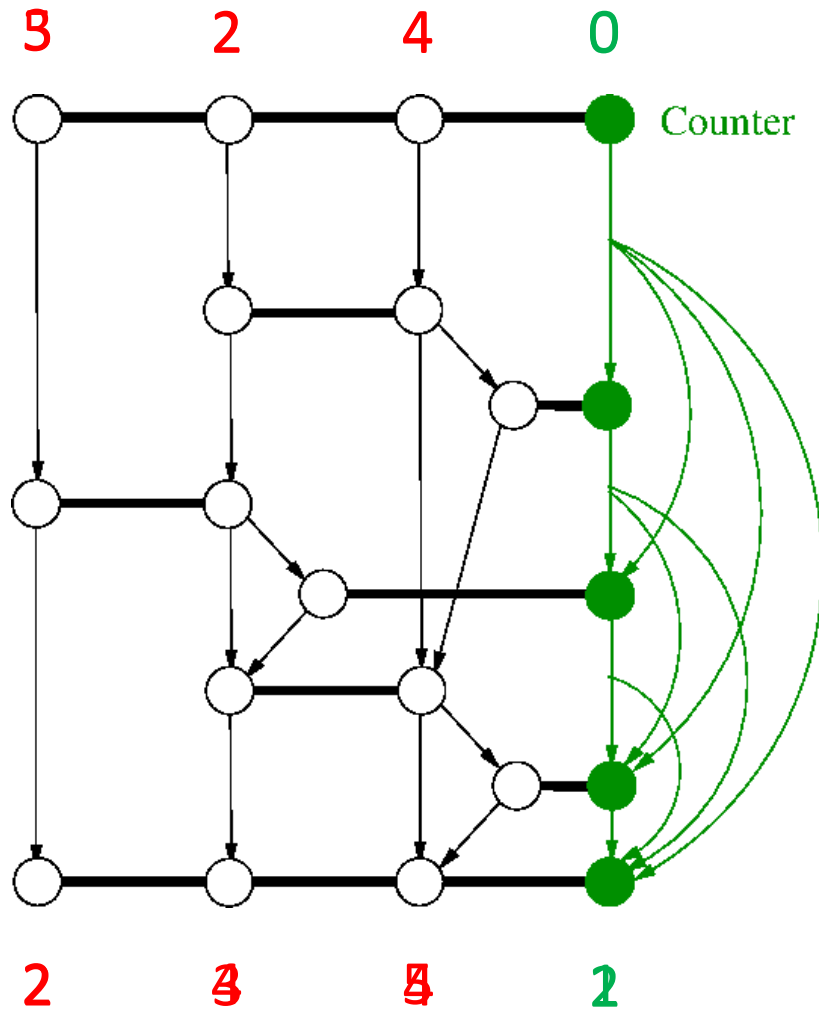
Parallel Bubblesort



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$T(x, y) = \text{if } y < x$
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else (x, y)

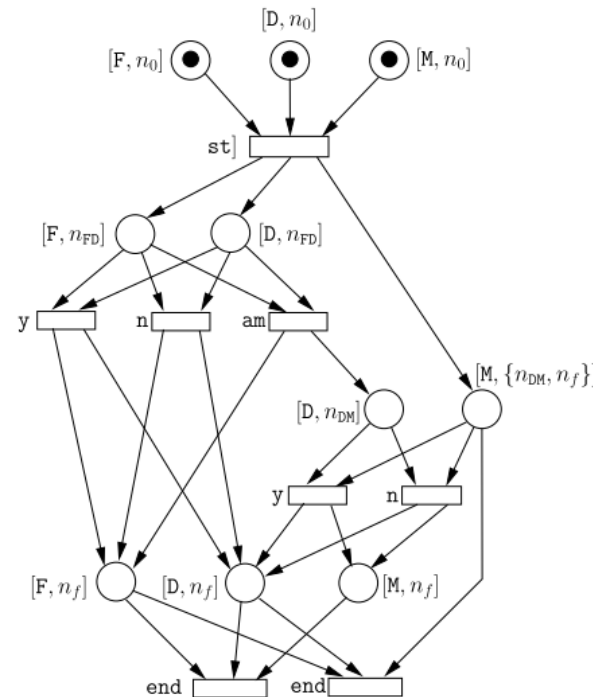
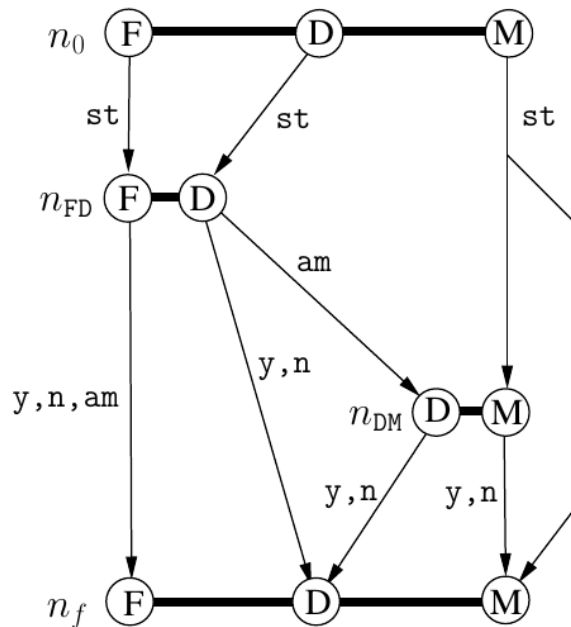
Counting pairs of consecutive numbers



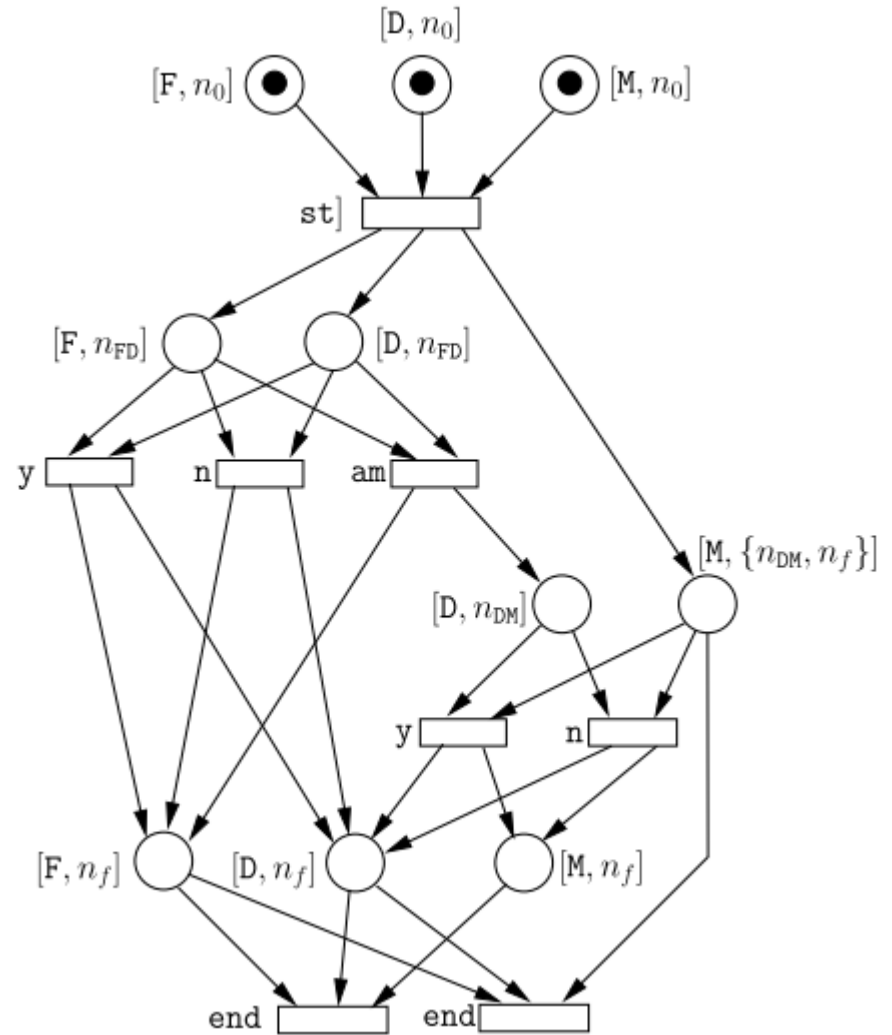
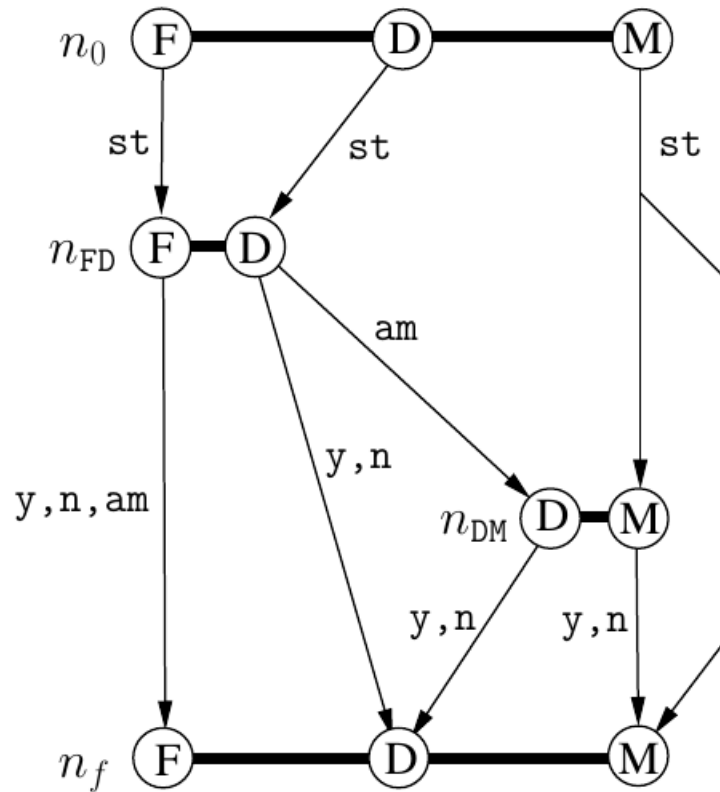
- Sort three integers and count the number of consecutive pairs
- Three agents communicate with a fourth Counter agent
- Is it correct ...?

Negotiations and Petri nets

- Negotiations have the same expressive power as (coloured) 1-safe Petri nets.
- However, negotiations can be exponentially more succinct.



Negotiations $\rightarrow$ 1-safe Petri nets



Negotiations $\rightarrow$ 1-safe Petri nets

$[D, n_{DM}]$

$[M, \{n_{DM}, n_f\}]$

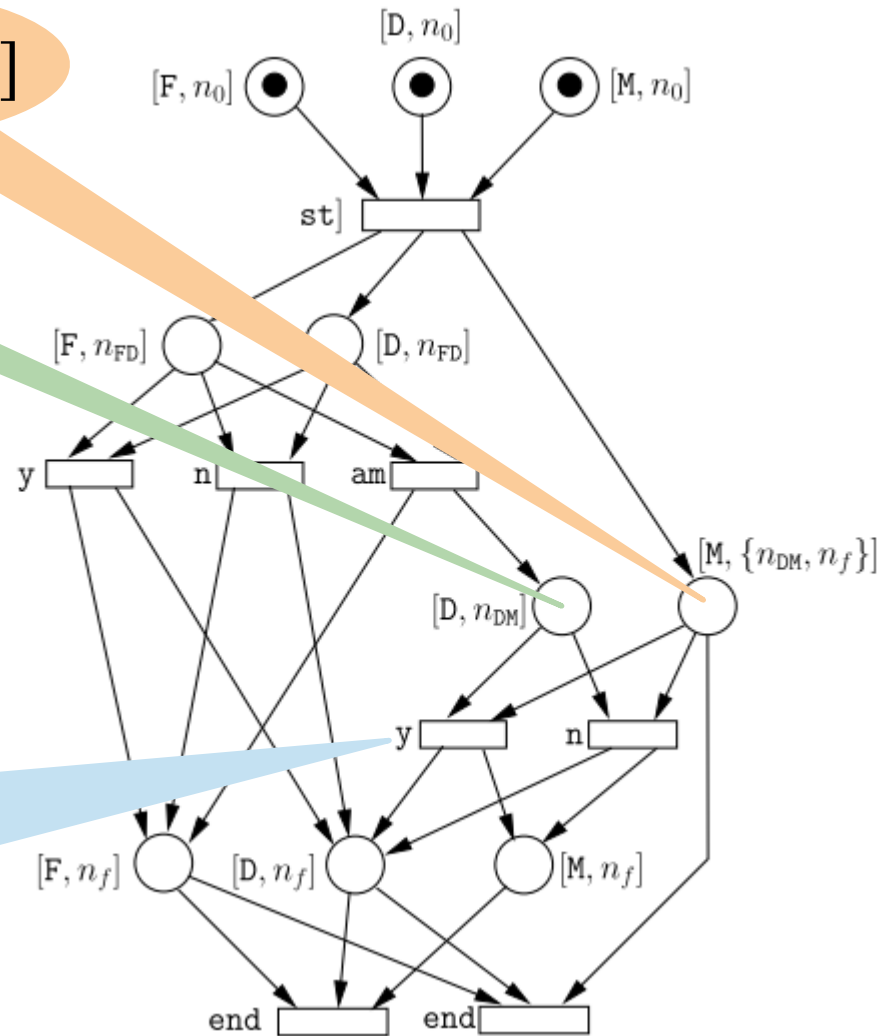
Meaning of a token in $[D, n_{DM}]$:

agent D is currently ready to engage in the atom n_{DM} (and no others)

Meaning of a token in $[M, \{n_{DM}, n_f\}]$:

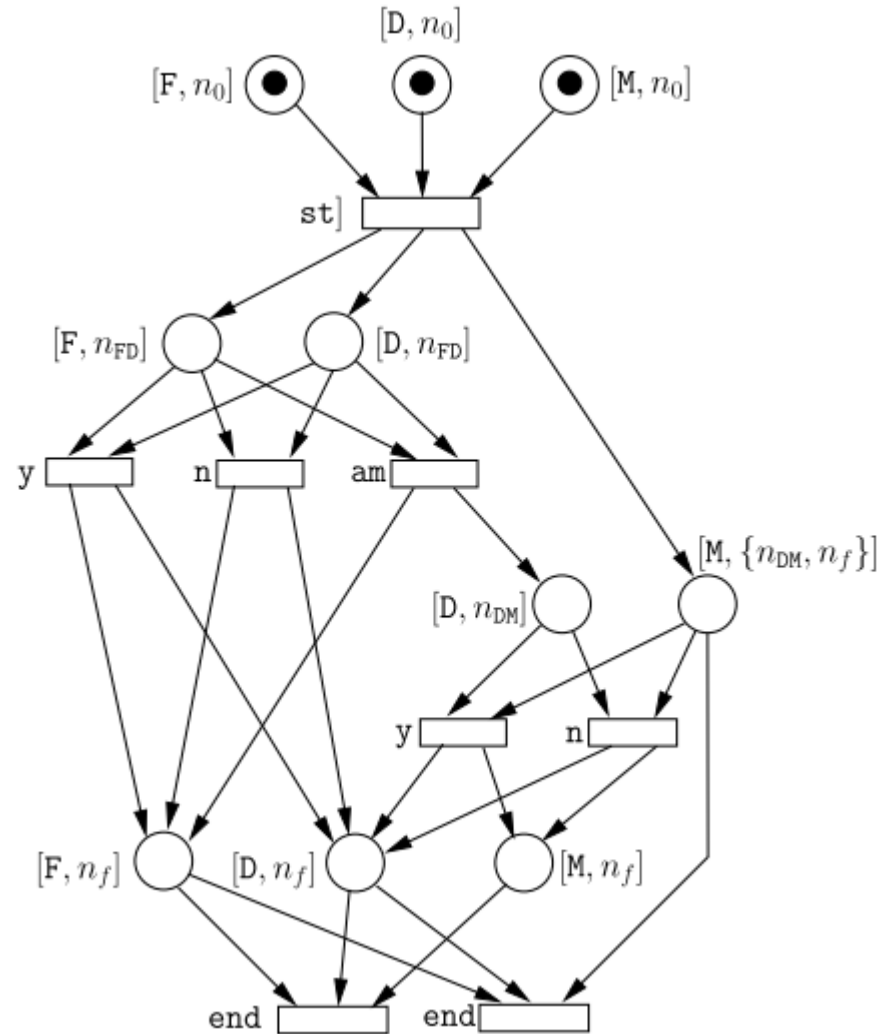
agent M is currently ready to engage in the atoms n_{DM} and n_f (and no others)

DM takes place with outcome „yes“, after which D and M are only ready to engage in n_f

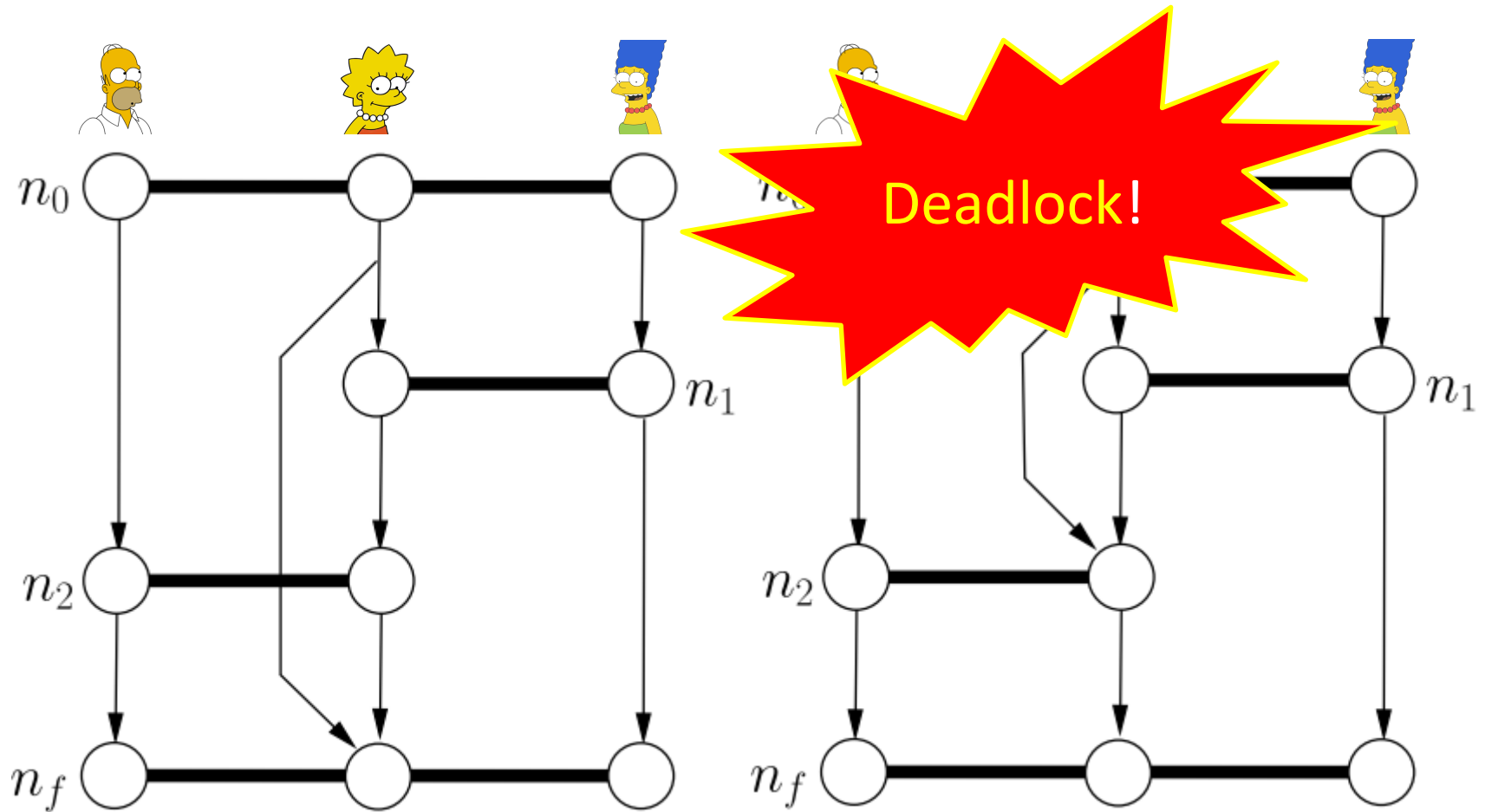


Negotiations $\rightarrow$ 1-safe Petri nets

- Places of the form $[\text{agent}, \text{set of atoms}] \Rightarrow$ number of places potentially exponential



Analysis problems: Soundness



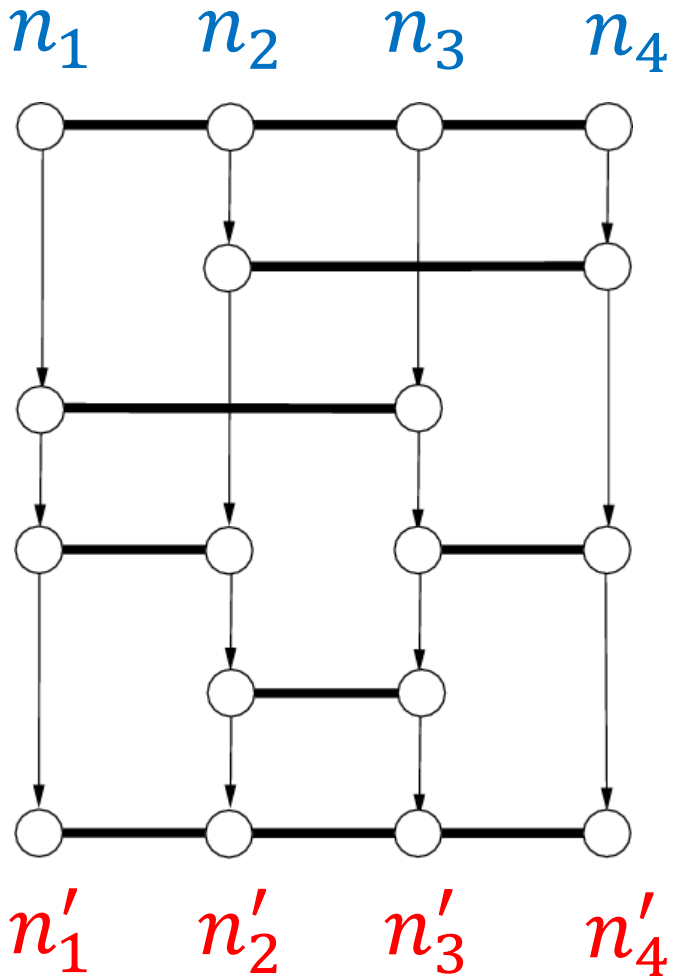
Analysis problems: Soundness

- **Large step:**
sequence of occurrences of atoms starting with the initial atom and ending with the final atom.
- A negotiation is **sound** if
 1. Every execution can be extended to a large step.
 2. No useless atoms: every atom occurs in some large step.(cf. van der Aalst's workflow nets)
- In particular: soundness $\rightarrow$ deadlock-freedom

Analysis problems: Summarization

- Each large step induces a relation between initial and final global states
- The **summary** of a negotiation is the union of these relations (i.e., the whole input-output relation).
- The **summarization problem** consists of, given a sound negotiation, computing its summary.

Analysis problems: Summarization



Sorting negotiation correct if

- sound, and
- summary consists of all pairs

((n_1, n_2, n_3, n_4) , (n'_1, n'_2, n'_3, n'_4))

such that $n'_1 n'_2 n'_3 n'_4$ is permutation of

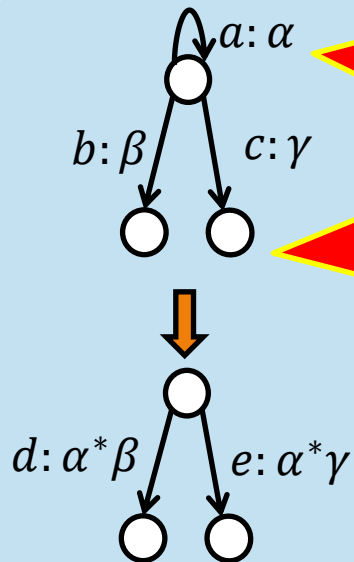
$n_1 n_2 n_3 n_4$ and $n'_1 \leq n'_2 \leq n'_3 \leq n'_4$

Computing summaries

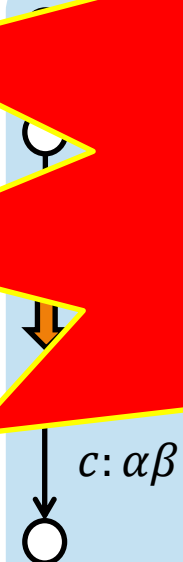
- A simple algorithm to compute a summary:
 - Compute the LTS of the negotiation
 - Apply **reduction rule**

$a: \alpha$
 $b: \beta$
 ...
 $e: \epsilon$

State explosion!



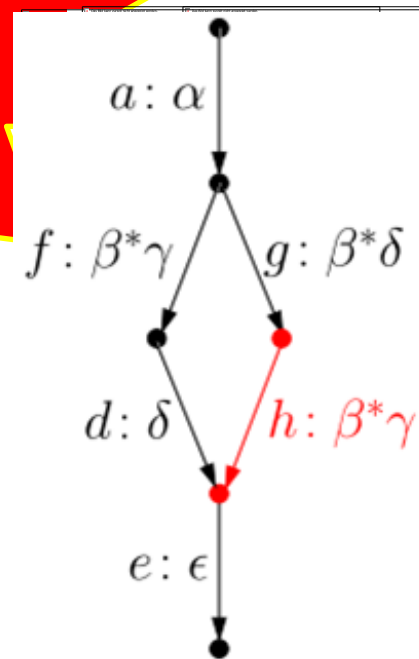
Iteration



Shortcut



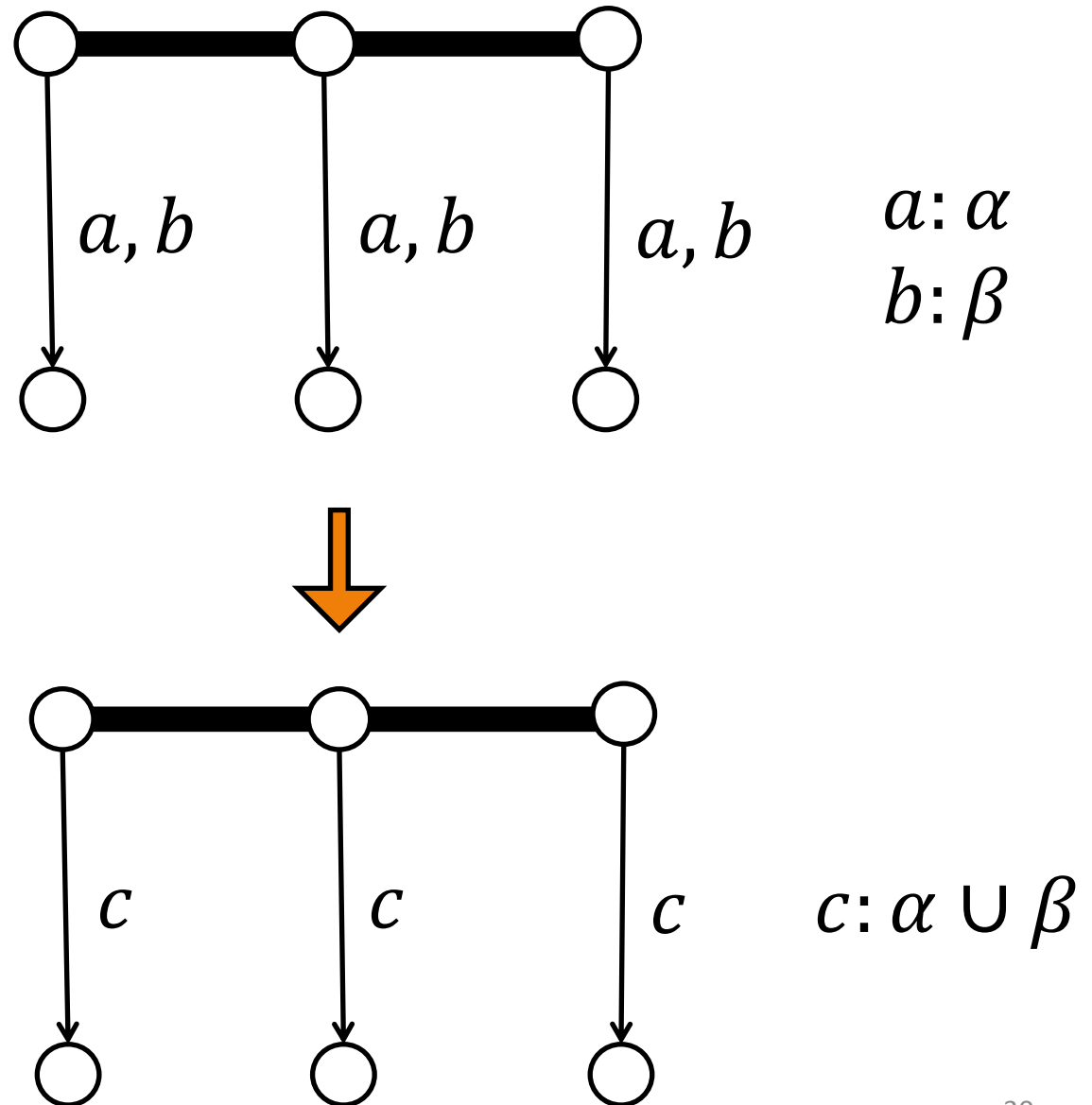
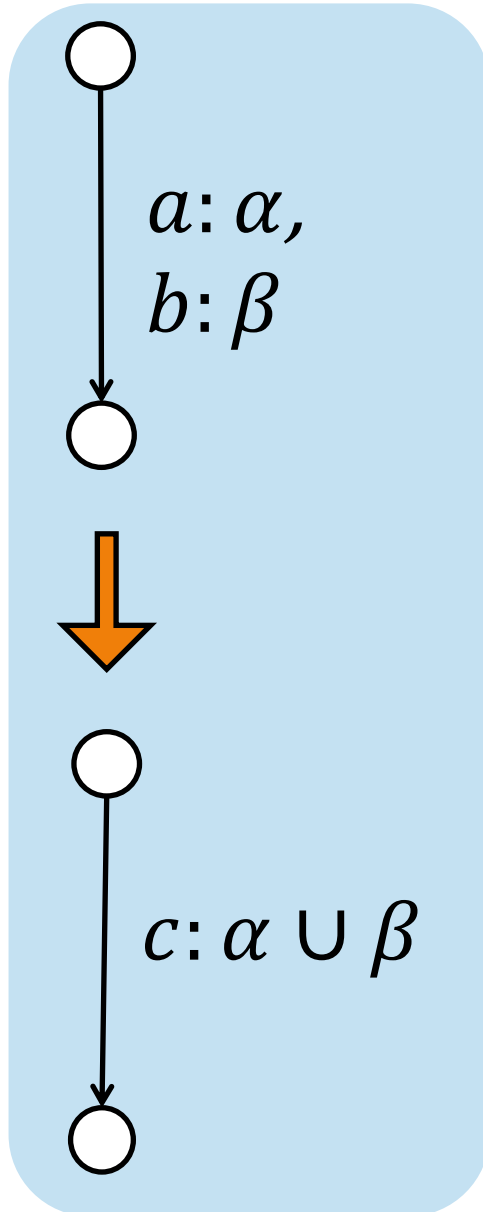
Merge



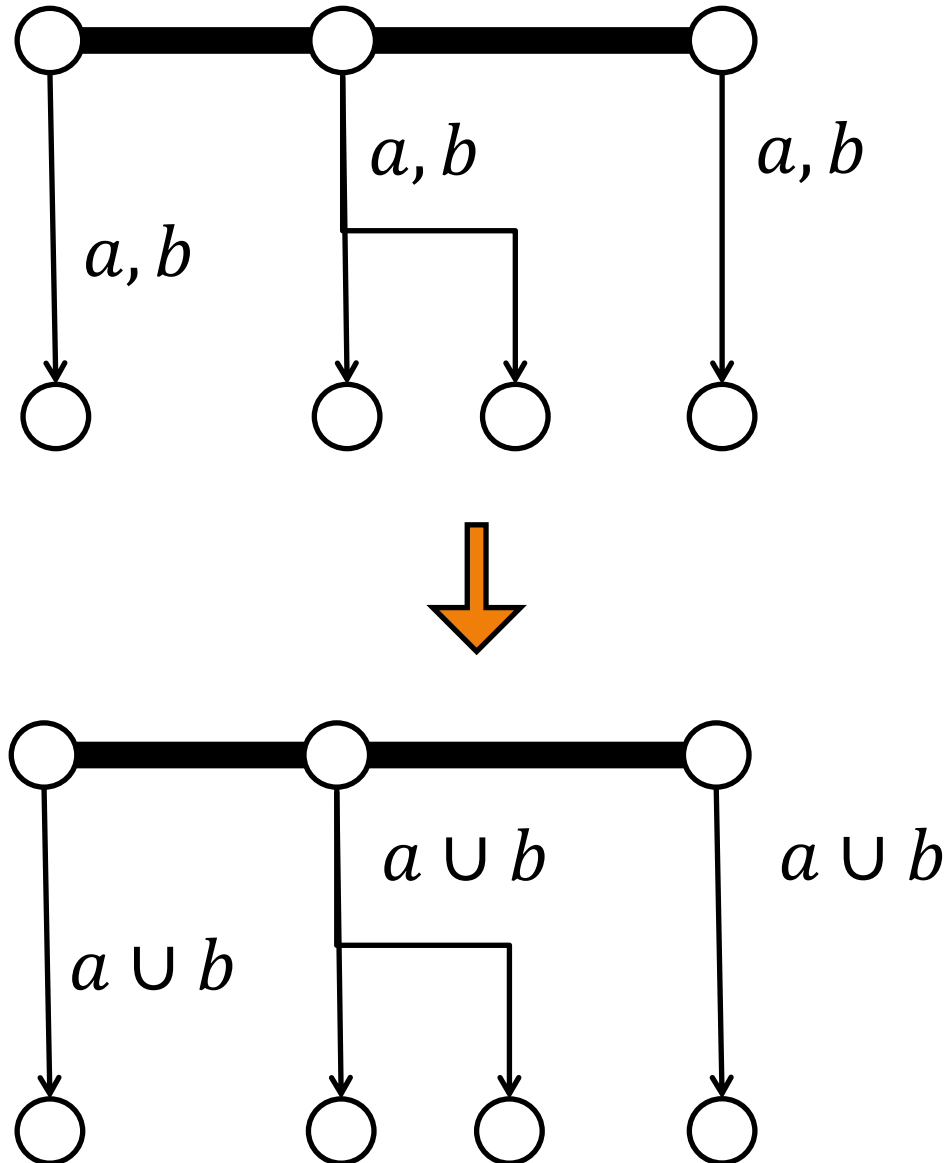
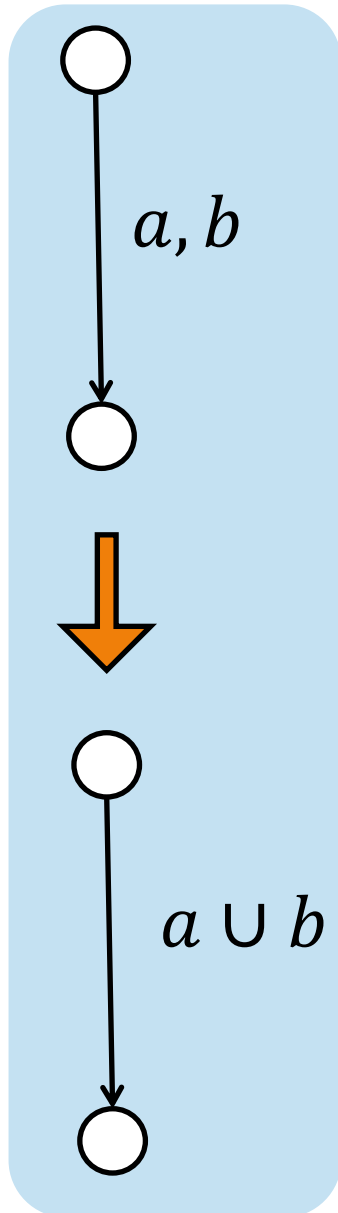
Reduction rules for negotiations

- Aim: find reduction rules
 - acting directly on negotiation diagrams (instead of their transition systems).
- Rules must:
 - preserve soundness:
sound after iff sound before
 - preserve the summary:
summary after equal to summary before
- We look for local rules:
application conditions and changes involve only a local neighbourhood of the application point.

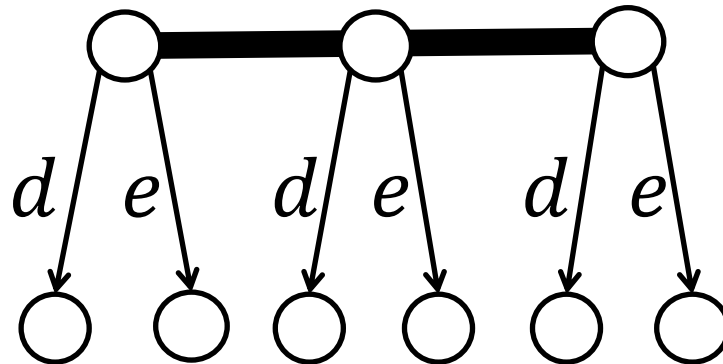
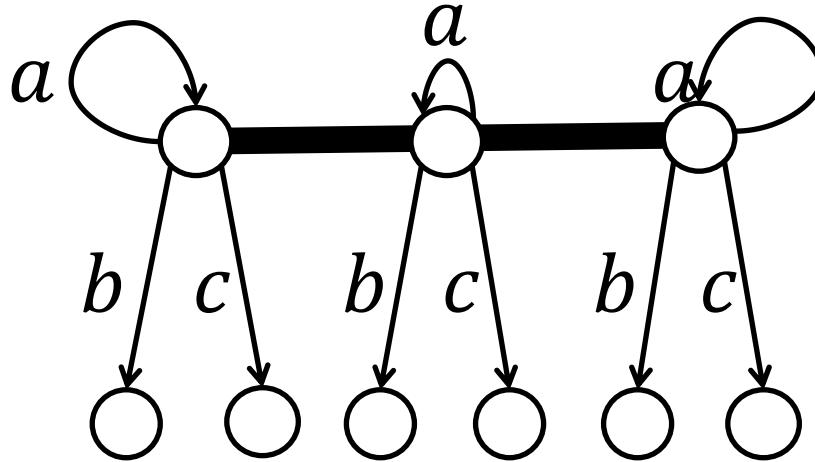
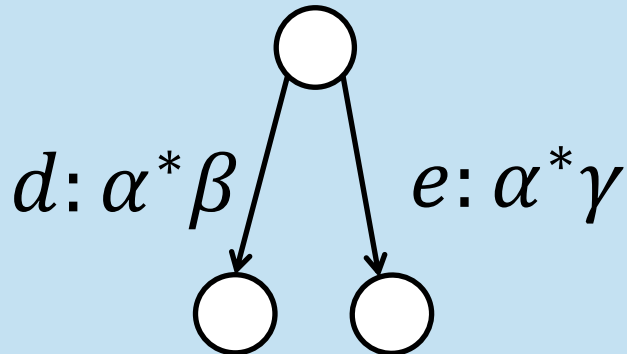
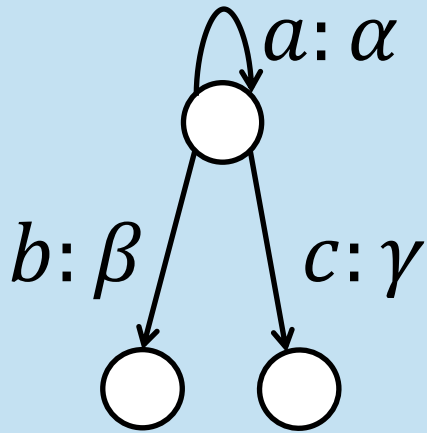
Rule 1: Merge



Rule 1: Merge



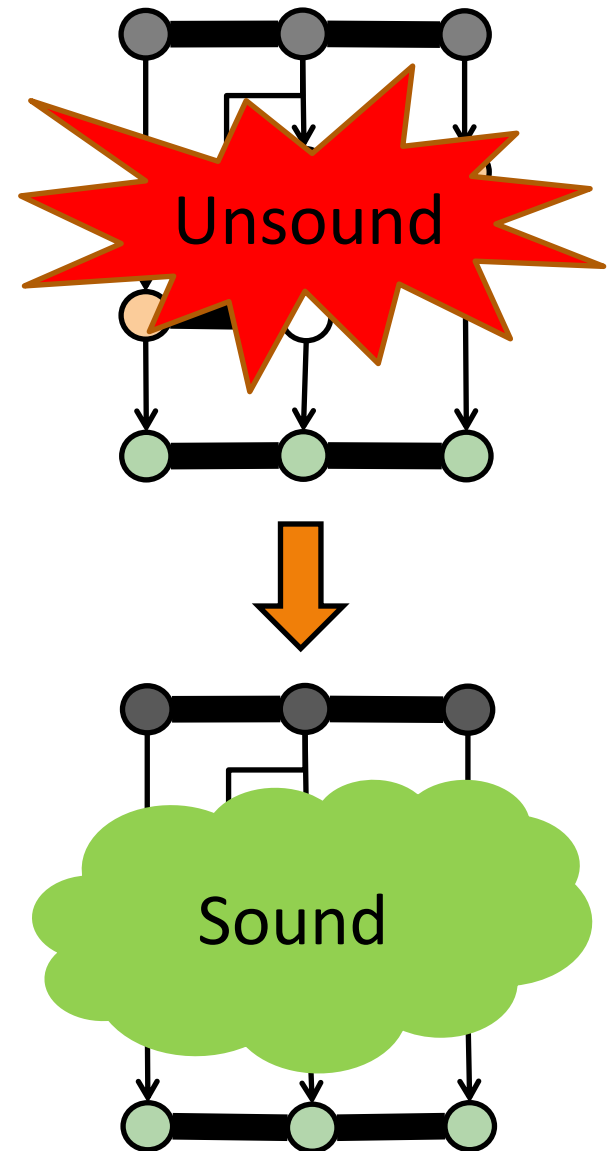
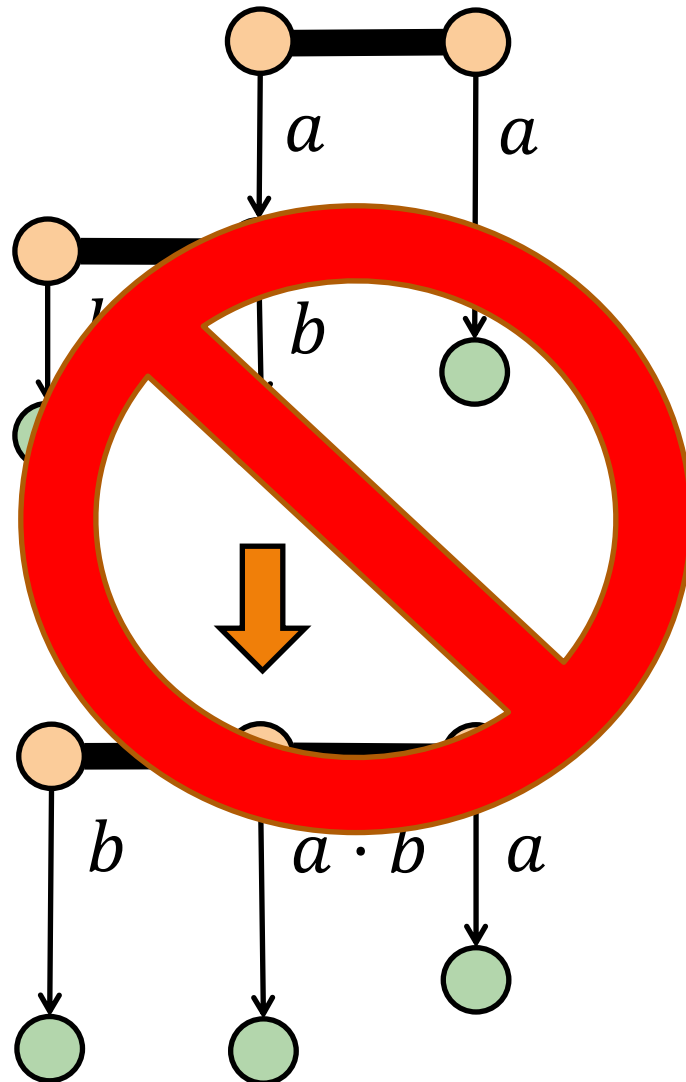
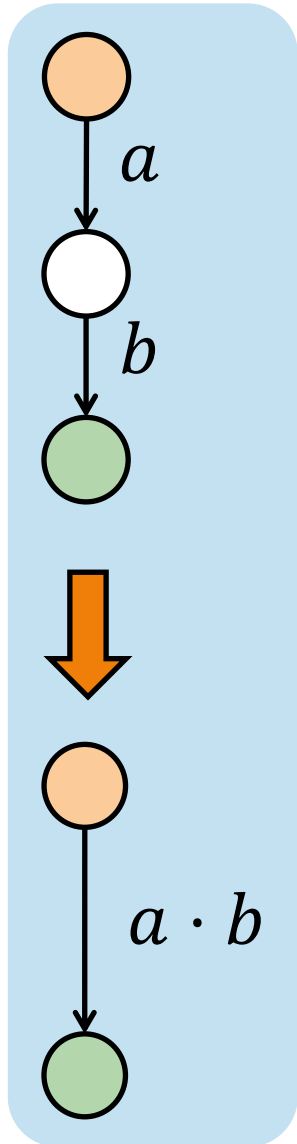
Rule 2: iteration



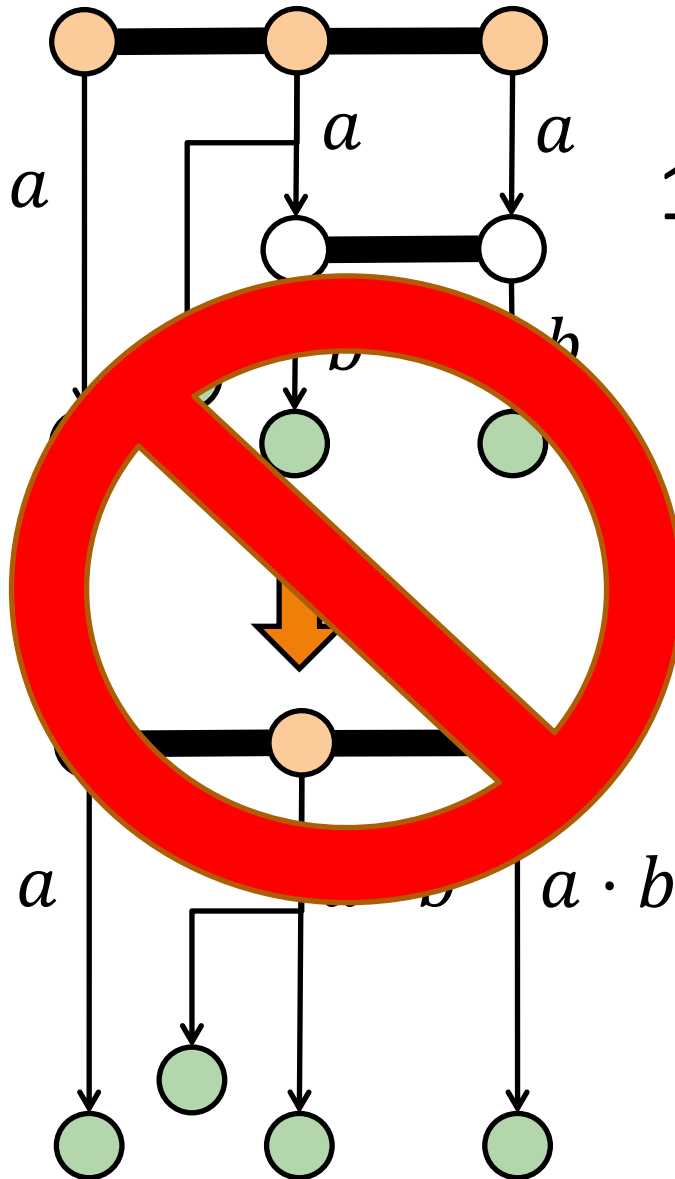
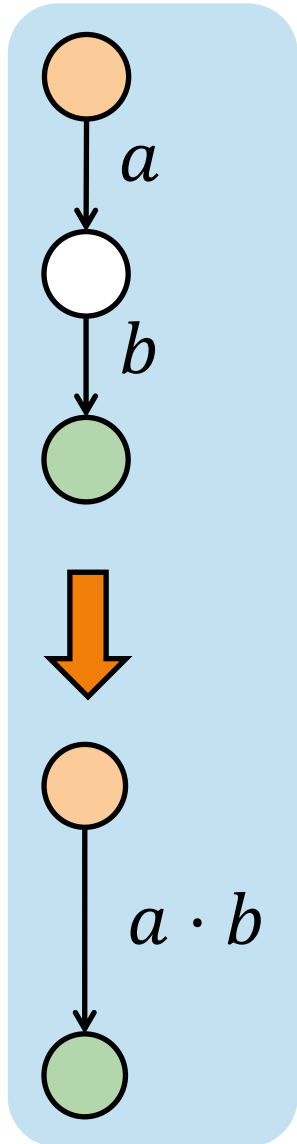
$a: \alpha$
 $b: \beta$
 $c: \gamma$

$d: \alpha^* \beta$
 $e: \alpha^* \gamma$

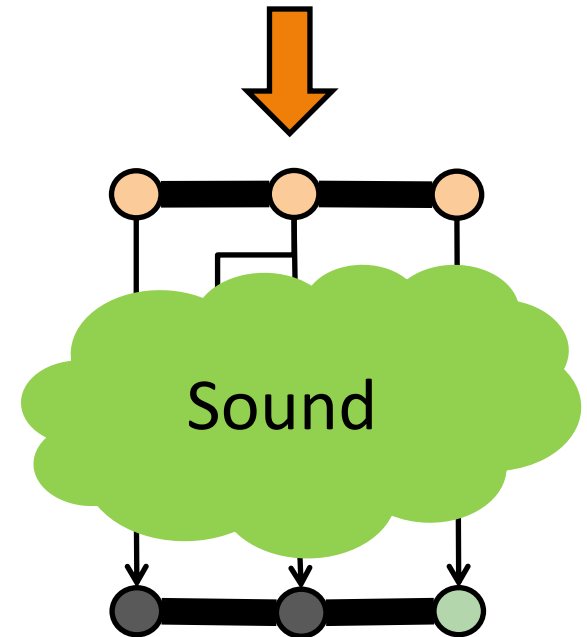
Rule 3: shortcut



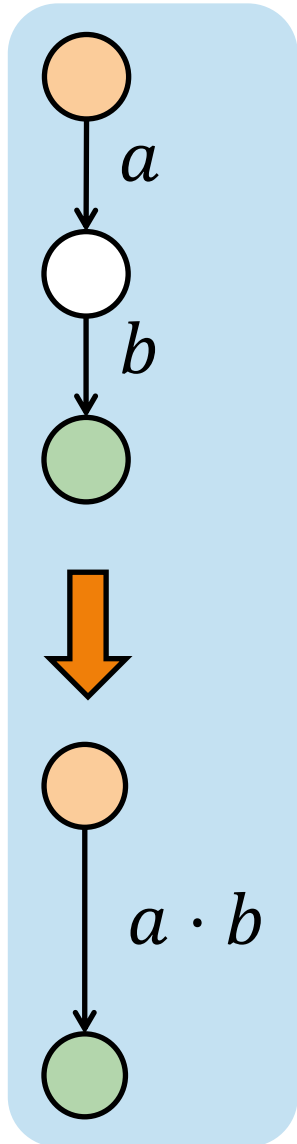
Rule 3: shortcut



1. **Unsound**
error in atom
unconditionally

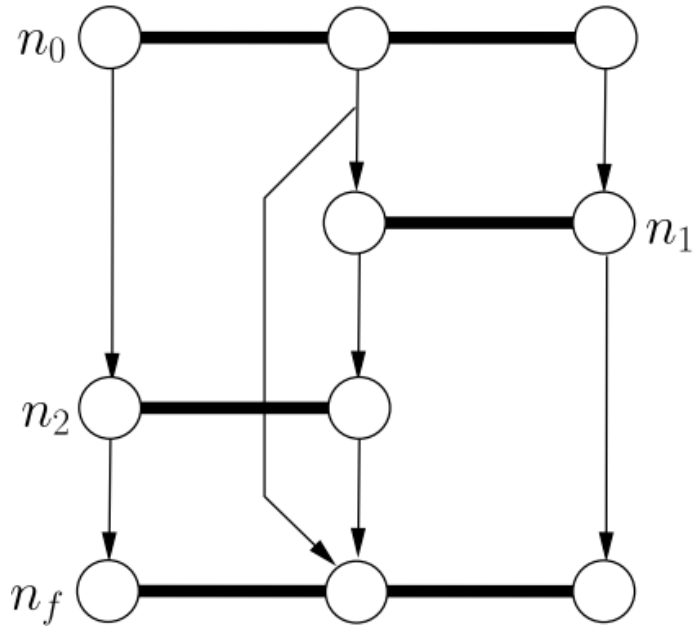


Rule 3: shortcut



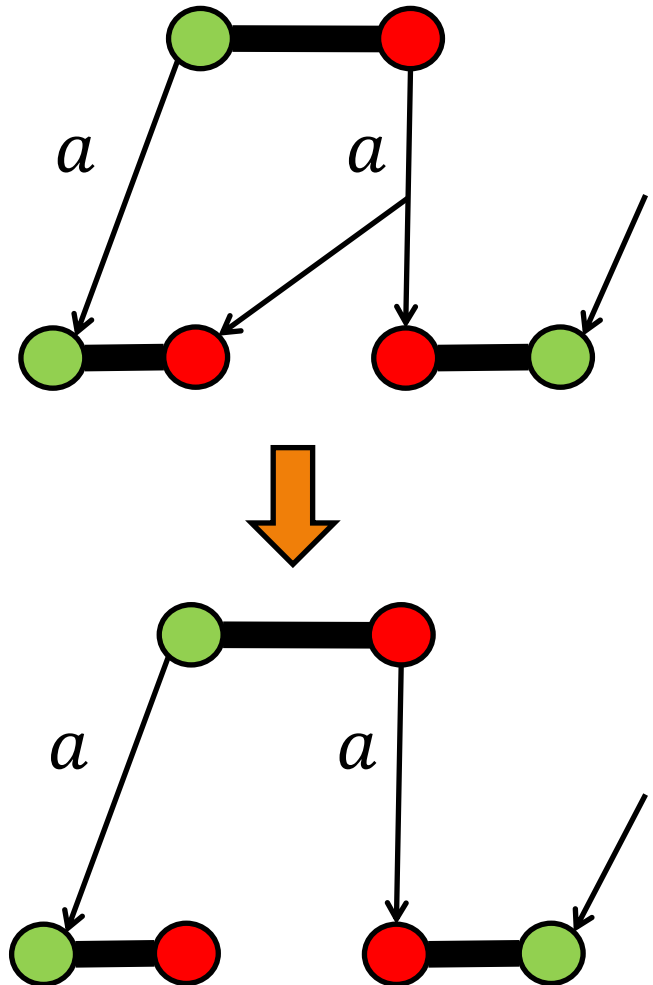
range atom enables
hite atom
conditionally.
forks from orange
white.
ne more technical
condition (see paper).

Rule 4: useless arc



● Agent 1

● Agent 2



Completeness and polynomiality

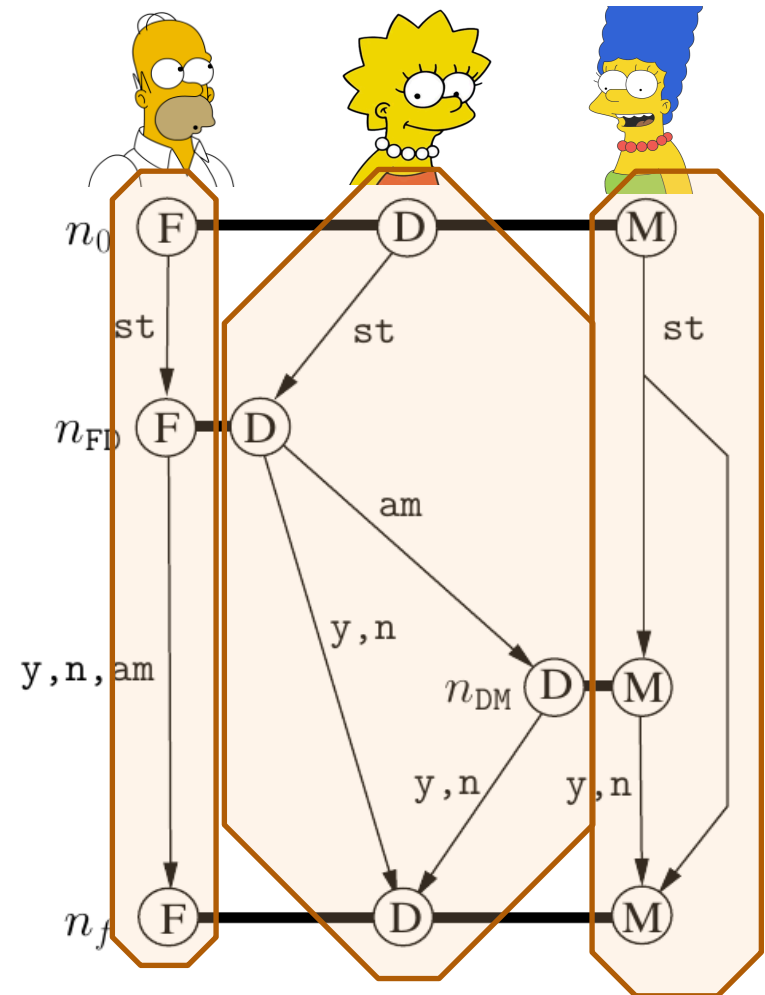
- A set of rules is **complete for a class** if it reduces all negotiations in the class to atomic negotiations.
- A complete set of rules is **polynomial** if every sound negotiation with k atoms is reduced to an atom by $p(k)$ rule applications, for some polynomial p .

Theorem [CONCUR 13]: deciding if a giving pair of global states belongs to the summary of a given negotiation is PSPACE-complete, even for every simple transformers.

Polynomiality and completeness results very unlikely for arbitrary negotiations.

Deterministic agents and negotiations

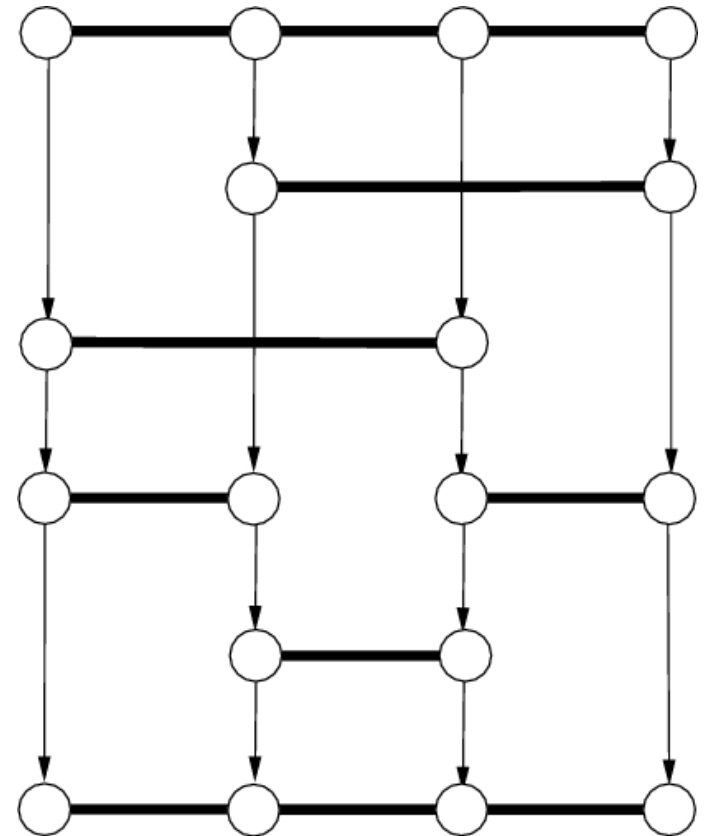
- An **agent** is **deterministic** if it is never ready to engage in more than one atom („no forks“).
- A **negotiation** is **deterministic** if every agent is deterministic.



non-deterministic

Deterministic agents and negotiations

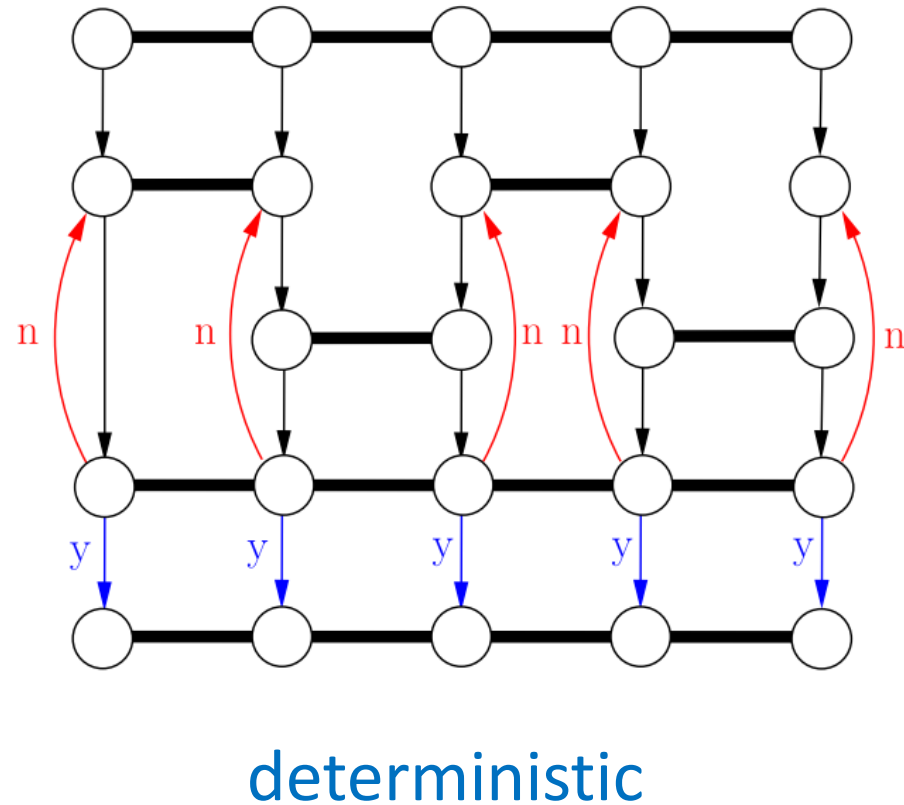
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deterministic

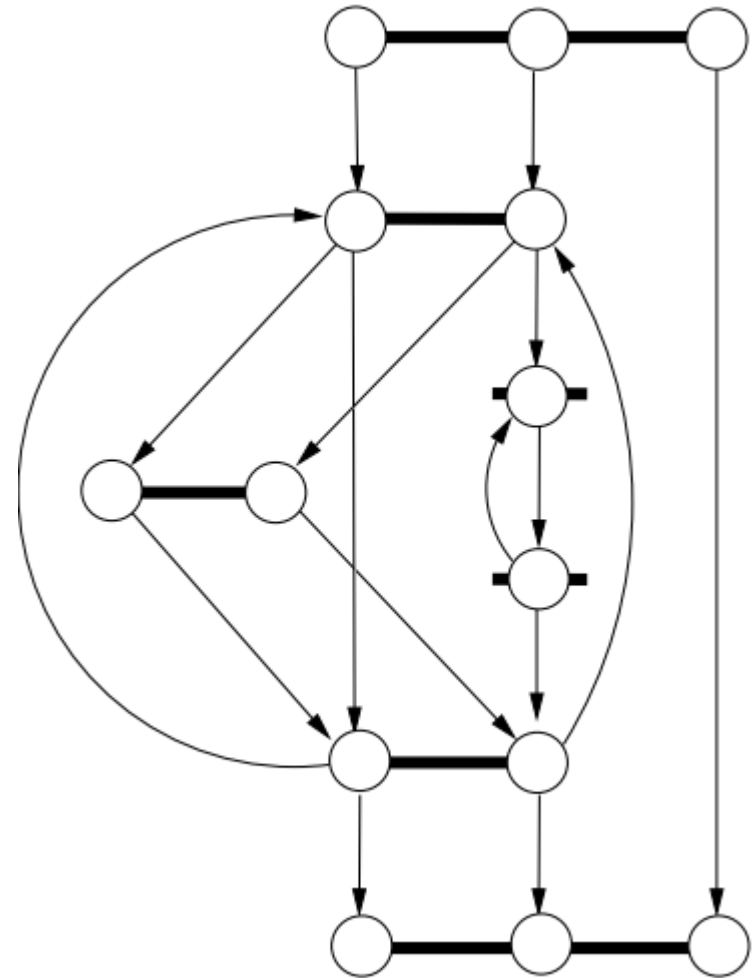
Deterministic agents and negotiations

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Deterministic agents and negotiations

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Deterministic negotiations: Results

- Theorem [CONCUR 13]:

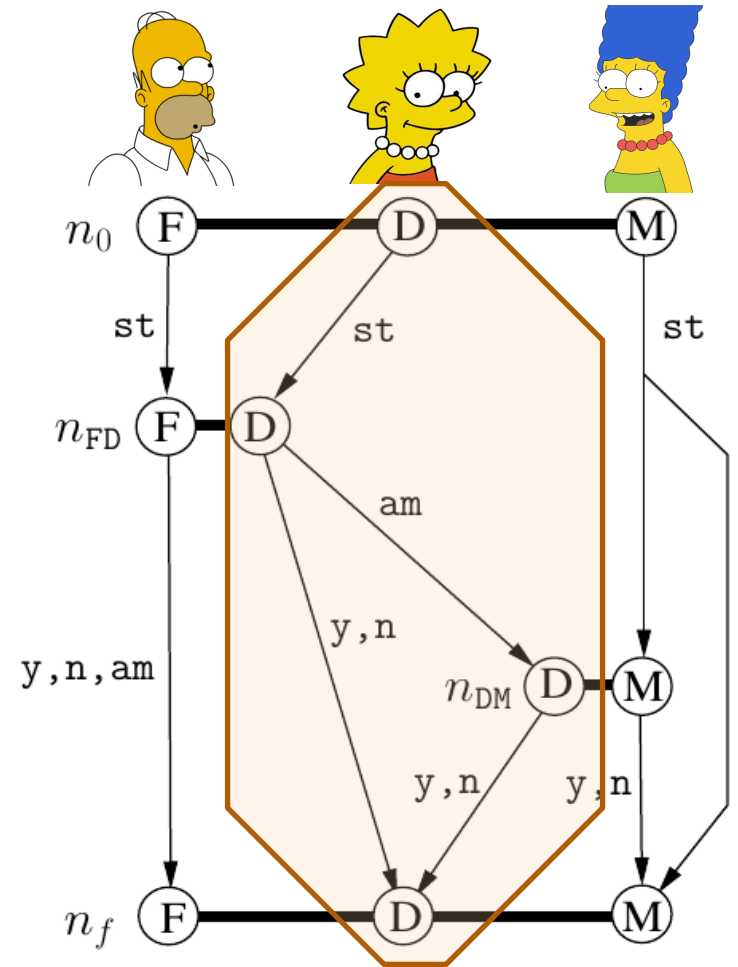
The shortcut and merge rules are complete and polynomial for acyclic deterministic negotiations

- Theorem [FOSSACS 14]:

The shortcut, merge, and iteration rules are complete and polynomial for arbitrary deterministic negotiations

Weakly deterministic negotiations

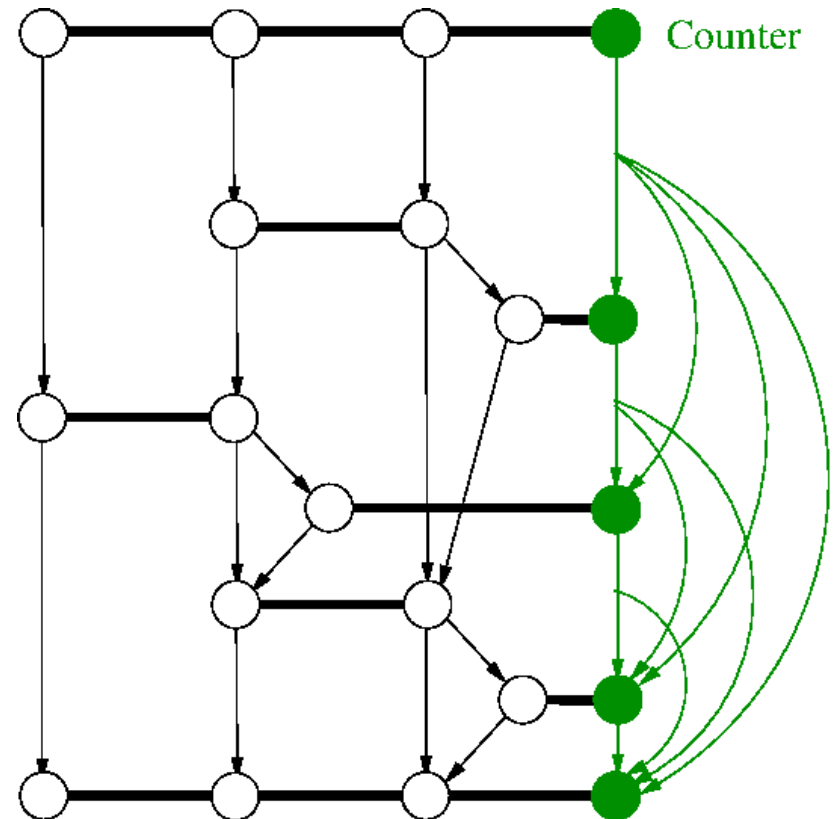
- A negotiation is **weakly deterministic** if every atom has a deterministic party



weakly deterministic

Weakly deterministic negotiations

- A negotiation is **weakly deterministic** if every atom has a deterministic party



weakly deterministic

Weakly Deterministic Negotiations: Results

- Theorem [CONCUR 13]:

The shortcut, merge, and useless arc rules are

complete for

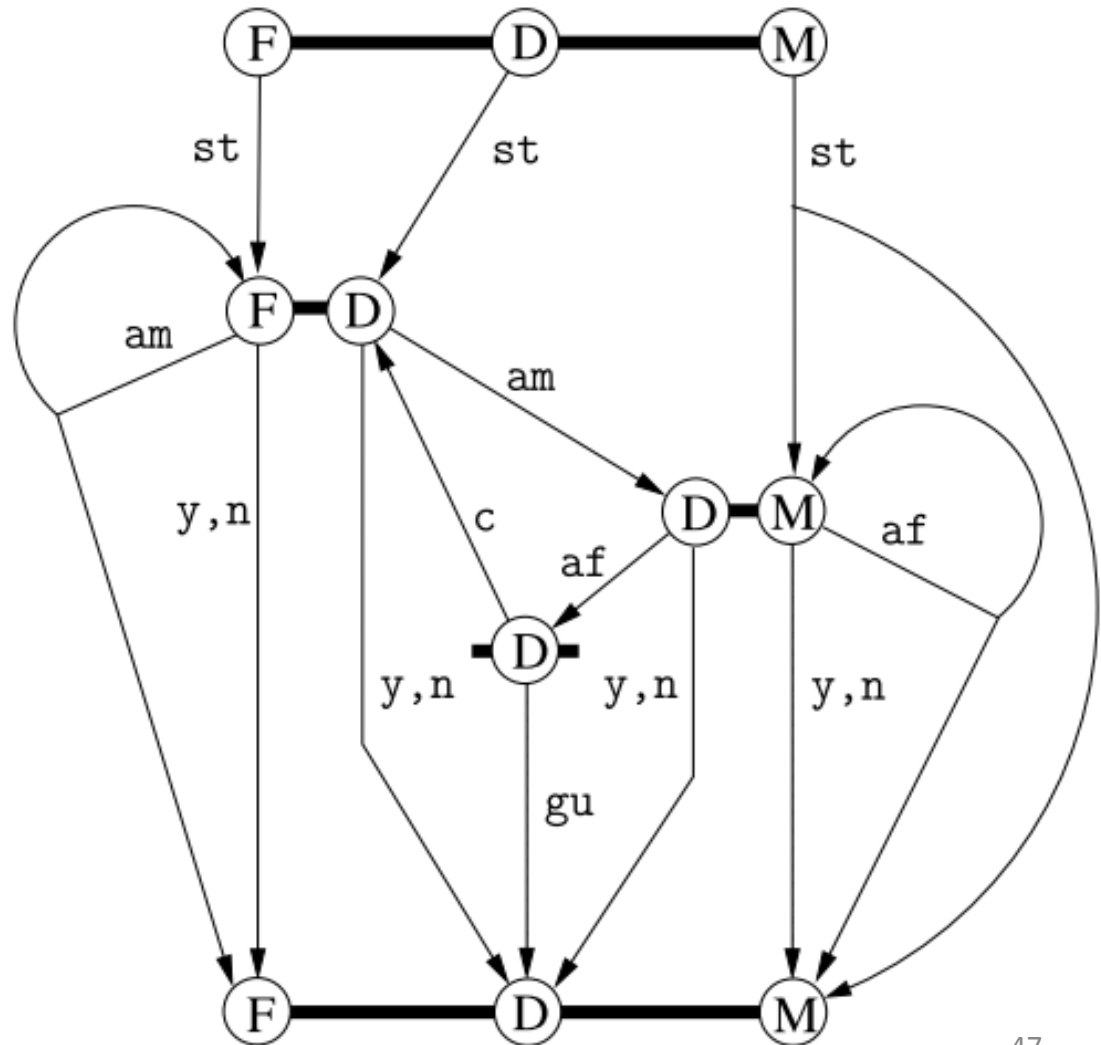
acyclic, weakly deterministic negotiations.

Deterministic negotiations: Results

- Theorem [FOSSACS 14]:
The shortcut, merge, and iteration rules are complete and polynomial for arbitrary deterministic negotiations

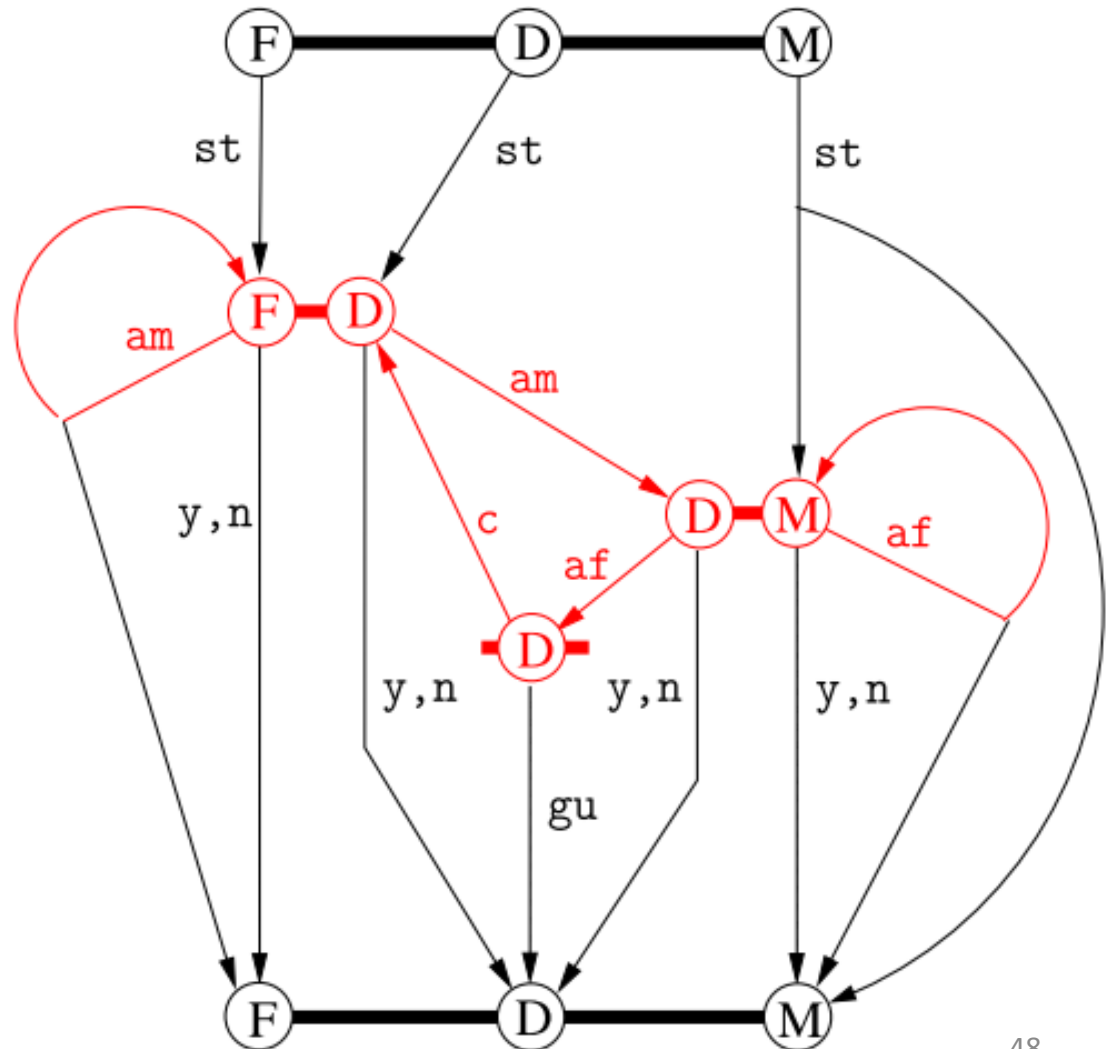
A Proof Sketch: Loop fragments

- A **loop** is a minimal firing sequence leading from a reachable marking to itself.



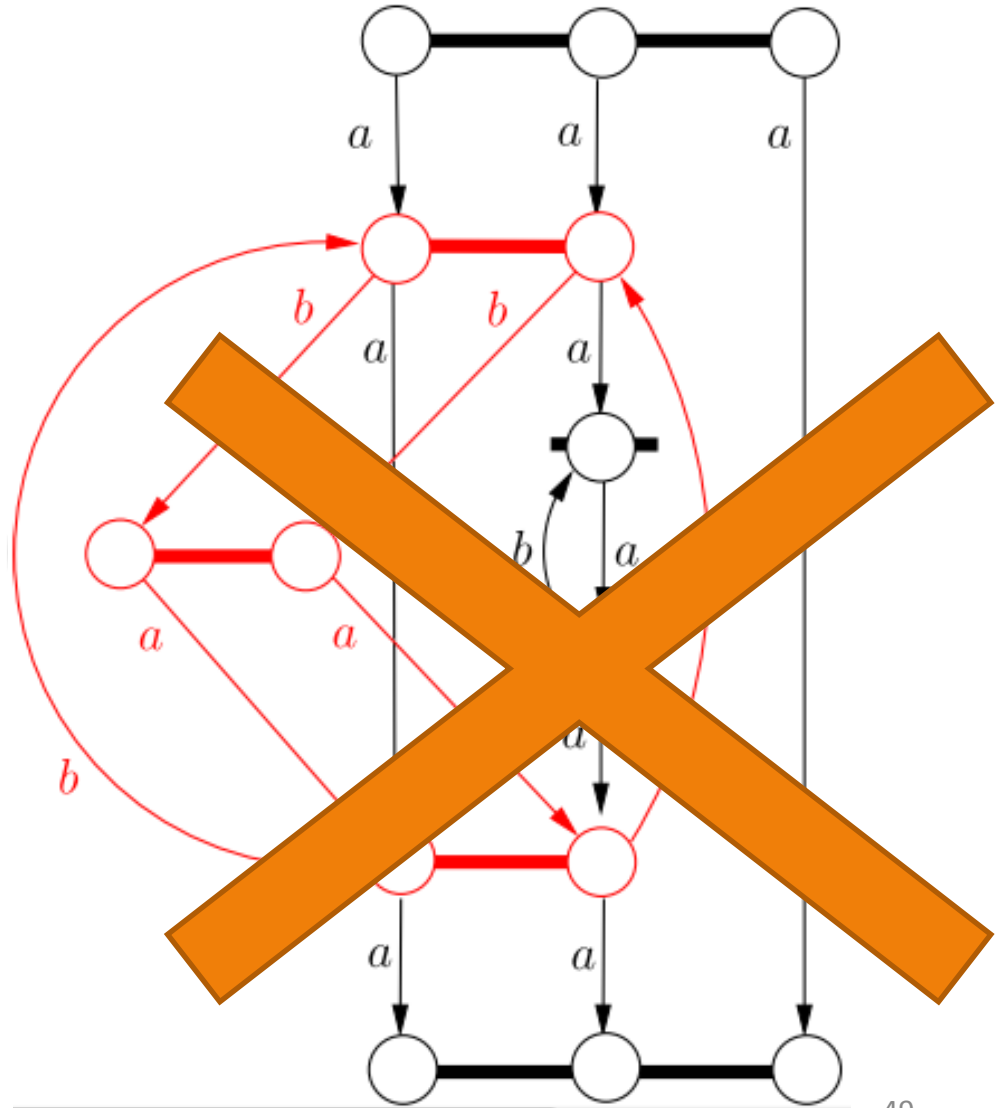
A Proof Sketch: Loop fragments

- A **loop** is a minimal firing sequence leading from a reachable marking to itself.
- A **loop fragment** is the subnegotiation that „occurs in the loop“



A Proof Sketch: Loop fragments

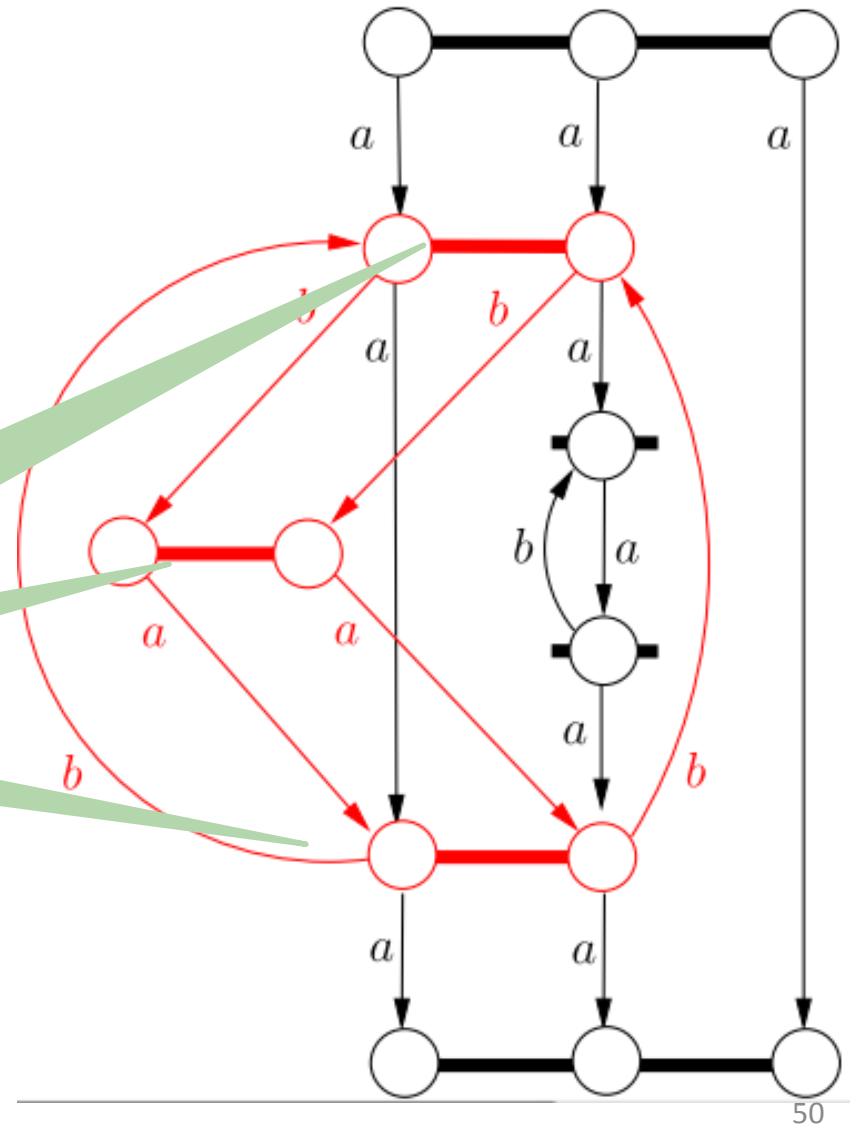
- A **loop** is a minimal firing sequence leading from a reachable marking to itself.
- A **loop fragment** is the subnegotiation that „occurs in the loop“



A Proof Sketch: Loop fragments

- **Lemma:** every loop fragment of a sound deterministic negotiation has a **synchronizer**

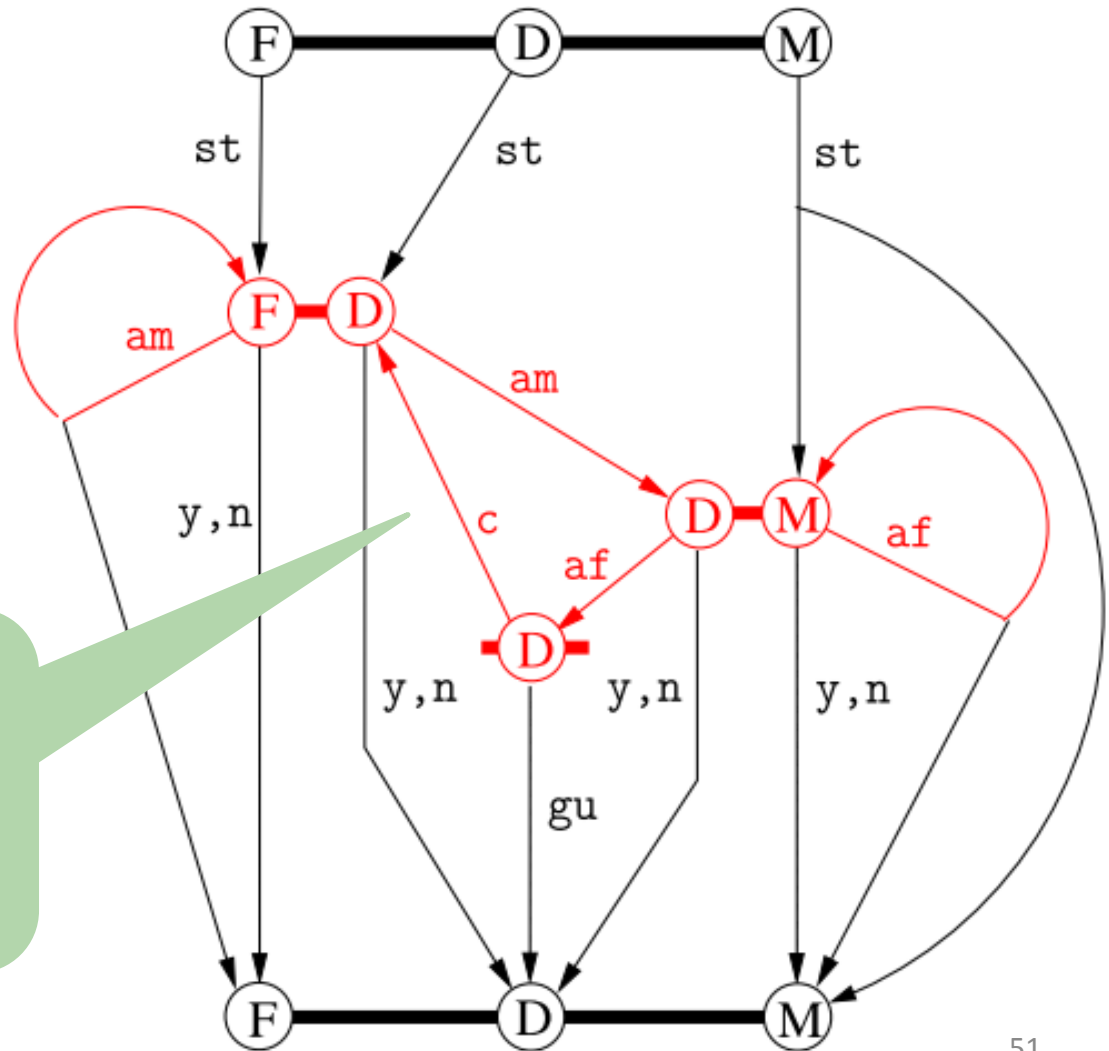
Synchronizers



A Proof Sketch: Loop fragments

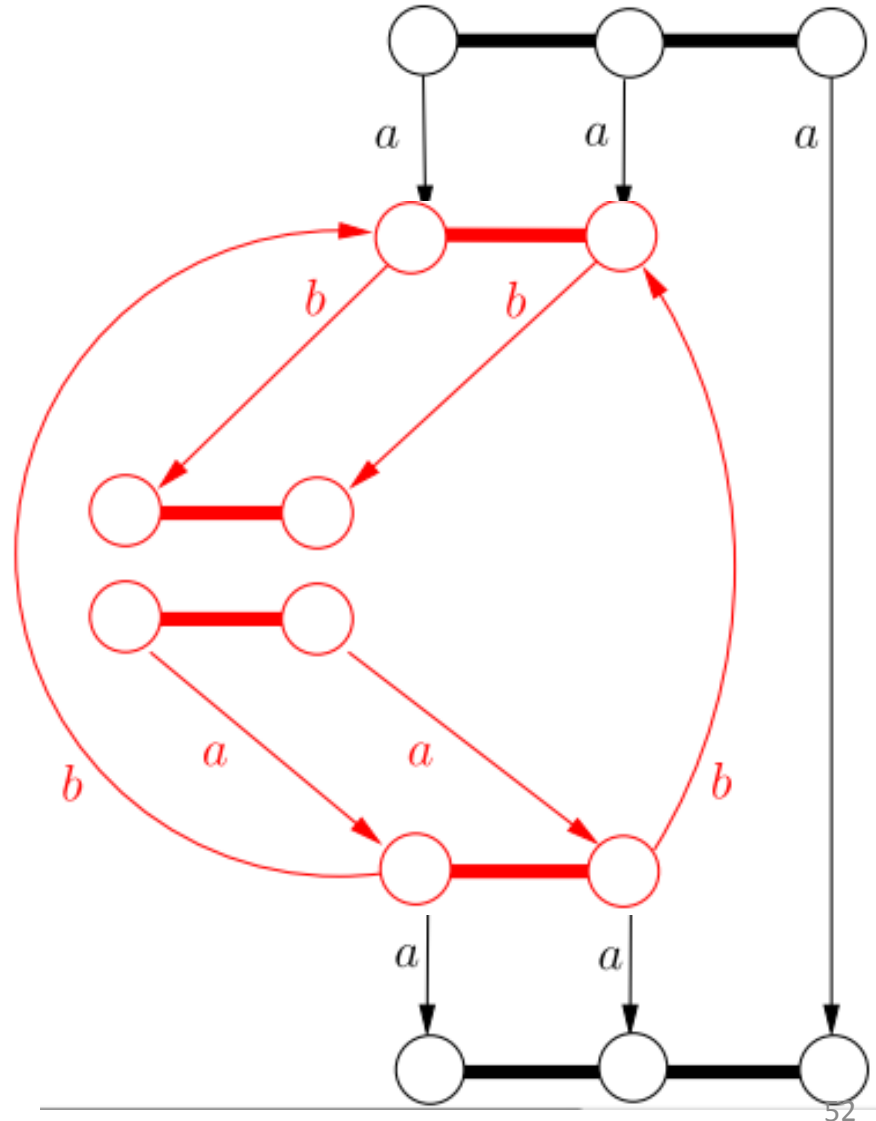
- **Lemma:** every loop fragment of a sound deterministic negotiation has a **synchronizer**

loop has no synchronizer, but negotiation is not deterministic



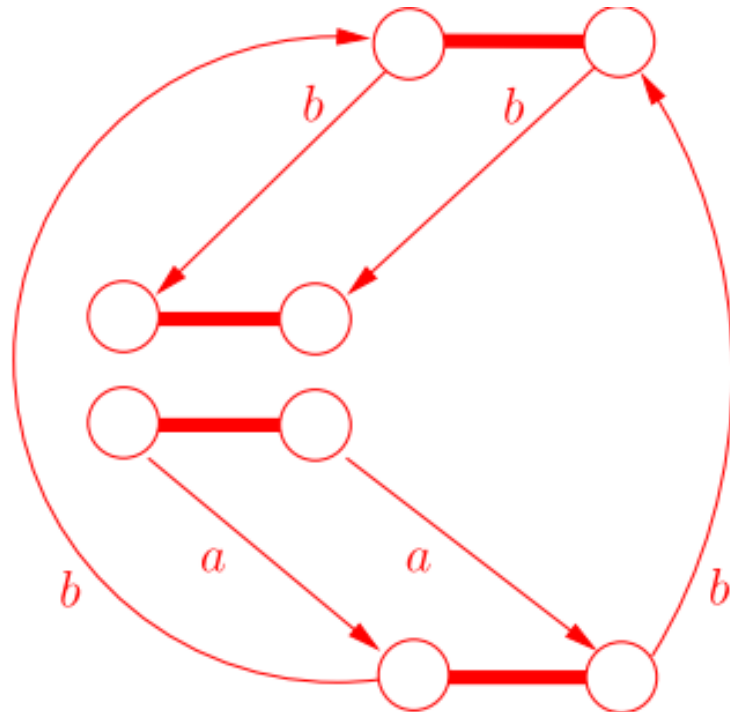
A Proof Sketch: Loop fragments

- Almost acyclic loop fragment: loop fragment that becomes acyclic after „cutting it along a synchronizer“



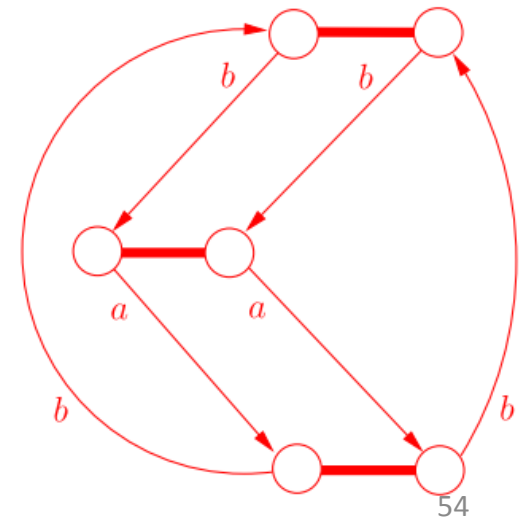
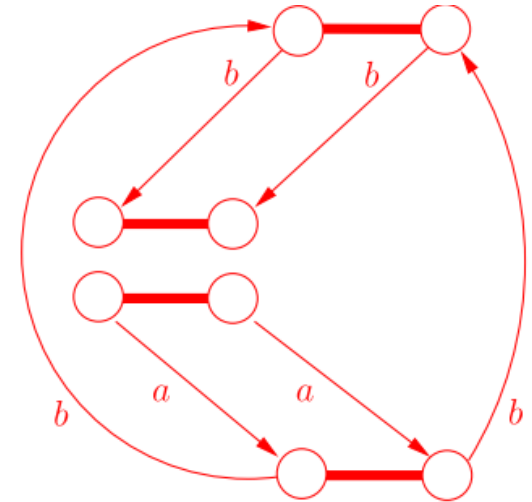
A Proof Sketch: Loop fragments

- **Almost acyclic loop fragment:** loop fragment that becomes acyclic after „cutting it along a synchronizer“
- **Lemma:** every cyclic, sound and deterministic negotiation contains an almost acyclic loop fragment.



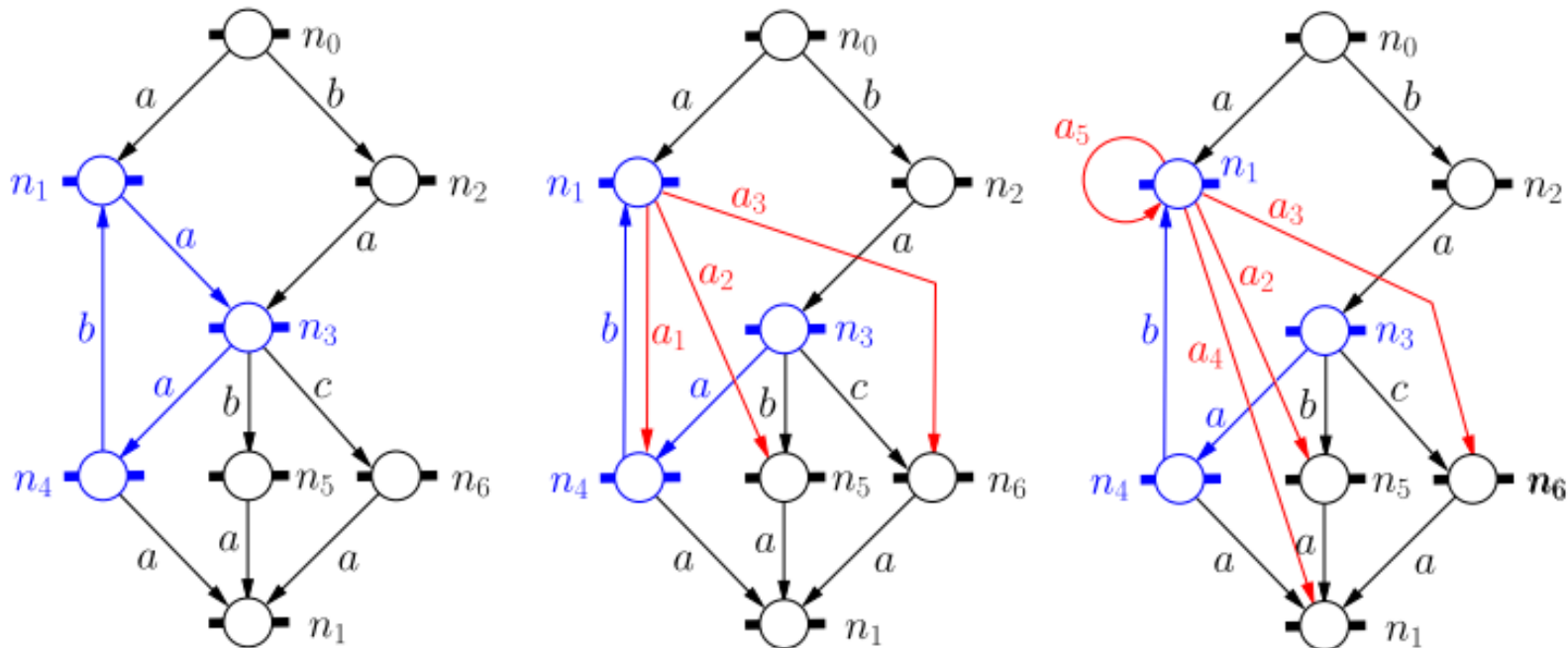
A Proof Sketch: Loop fragments

- **Theorem [CONCUR 13]:** Acyclic sound and deterministic negotiations can be reduced using the shortcut and merge rules.
- **Corollary:** loop fragments can be reduced to a „self-loop“ using the shortcut and merge rules. The self-loop can be reduced with the iteration rule.



A Proof Sketch: Polynomiality

- **Problem:** the reduction of a loop fragment to a self-loop produces „side-effects“



- Careful analysis required to ensure polynomiality.

A Proof Sketch: Polynomiality

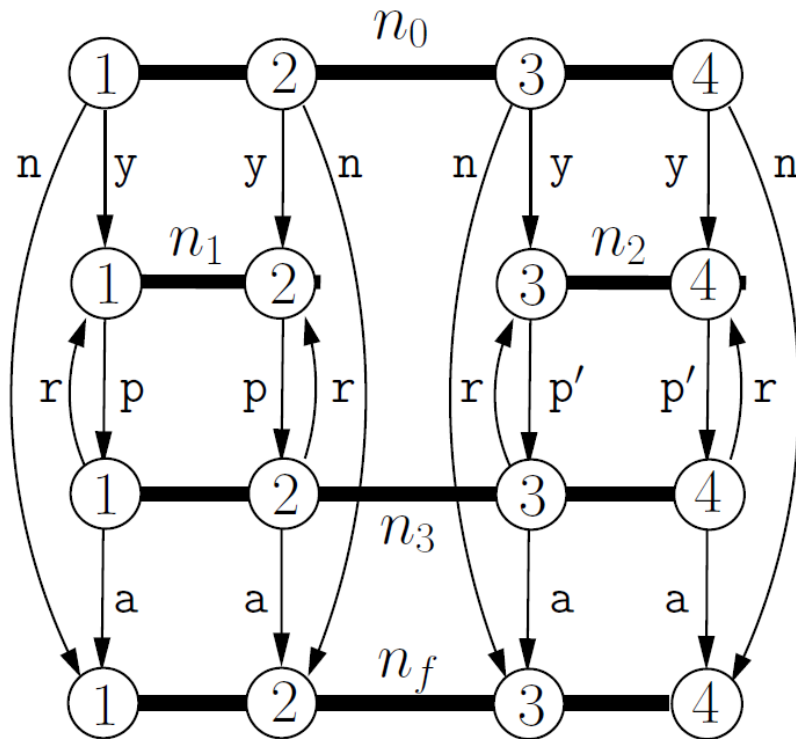
- **Theorem:** a sound and deterministic negotiation with n atoms and k outcomes can be reduced by means of $O(n^4k)$ applications of the shortcut, merge, and iteration rules.
- **Conjecture:** $O(n^2k)$ applications suffice.

New paper: Negotiation Programs

How can we implement negotiations?

How can we implement sound negotiations?
(correct by construction)

Negotiation Programs: an example

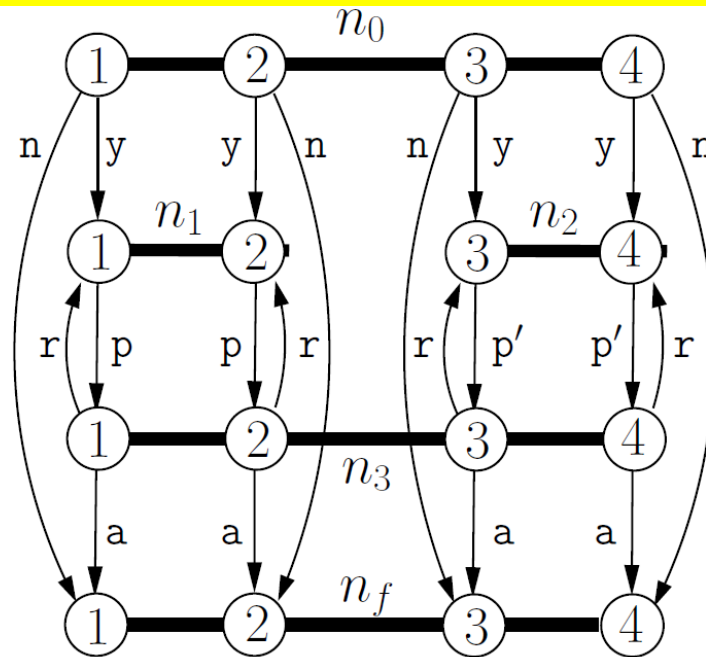


- n_0 : discuss a proposal?
- n_1 : team A makes plan.
- n_2 : team B makes plan.
- n_3 : plans are consistent?
- n_f : termination

Negotiation Programs: an example

```
agent   $a_1, a_2, a_3, a_4$ 
actions   $y, n, a, r : \{a_1, \dots, a_4\}; p : \{a_1, a_2\}; p' : \{a_3, a_4\}$ 
do  []  $y : (p \parallel p') \circ$ 
      do  $a$ :end  []  $r : (p \parallel p') \text{ loop od}$  end
    []  $n$ :end
od
```

Negotiation Programs: an example



agent a_1, a_2, a_3, a_4

actions $y, n, a, r : \{a_1, \dots, a_4\}; p : \{a_1, a_2\}; p' : \{a_3, a_4\}$

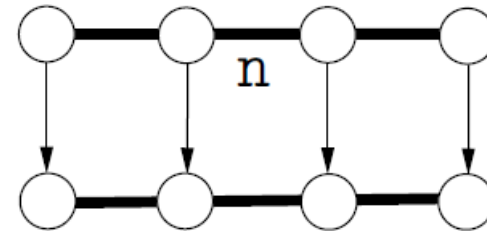
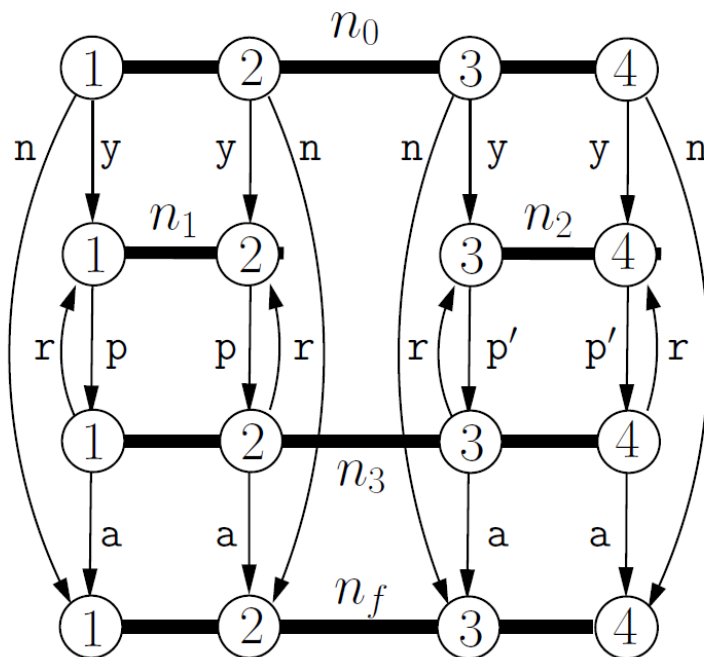
do $\square y : (p \parallel p') \circ$

do $a : \text{end} \square r : (p \parallel p') \text{ loop od end}$

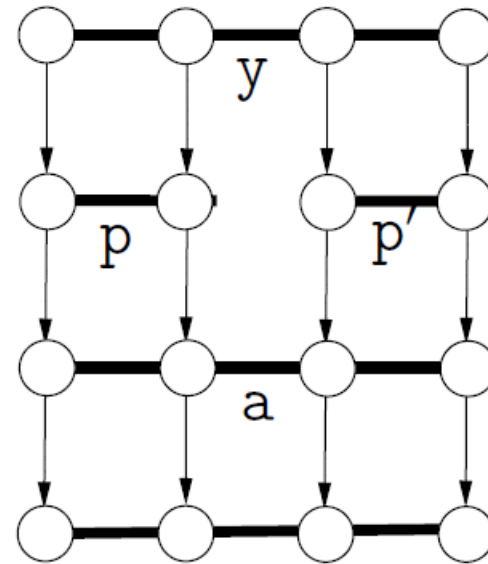
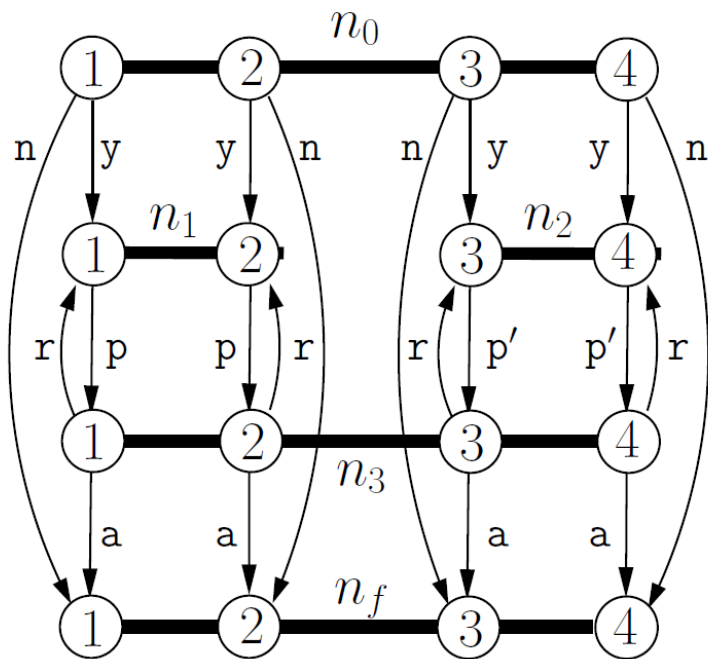
$\square n : \text{end}$

od

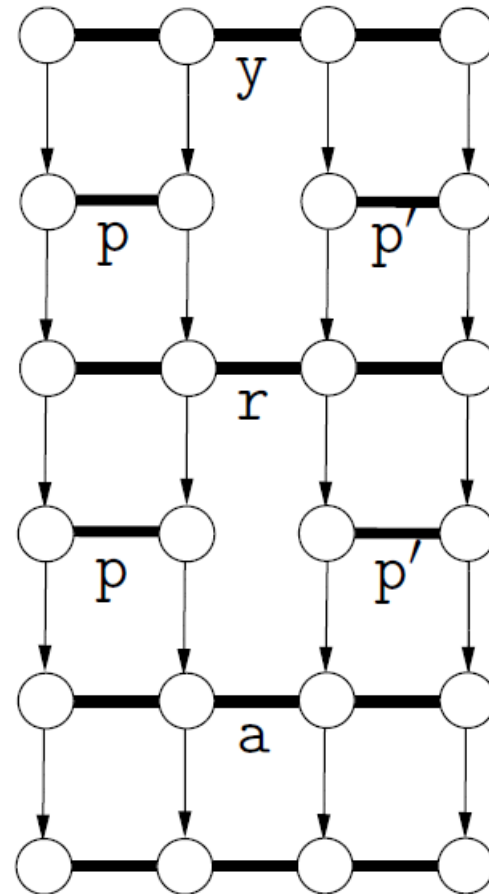
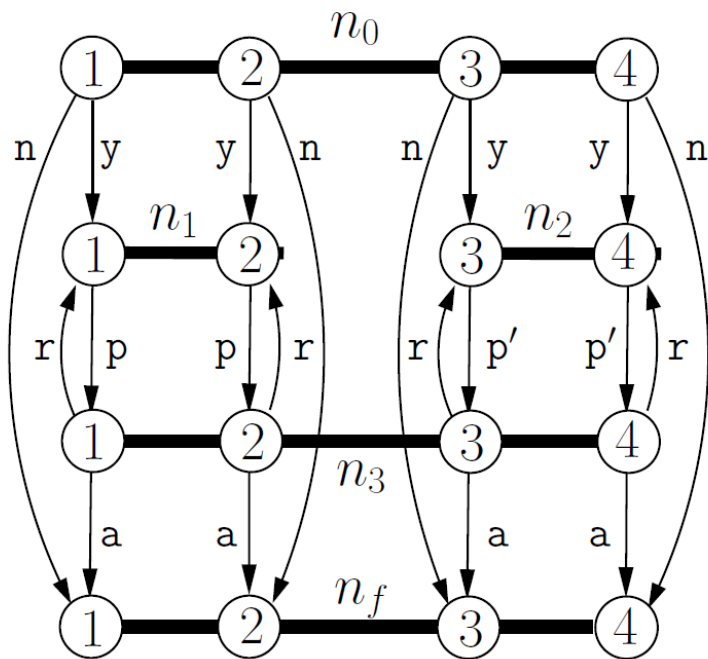
Semantics of negotiations: Mazurkiewicz traces



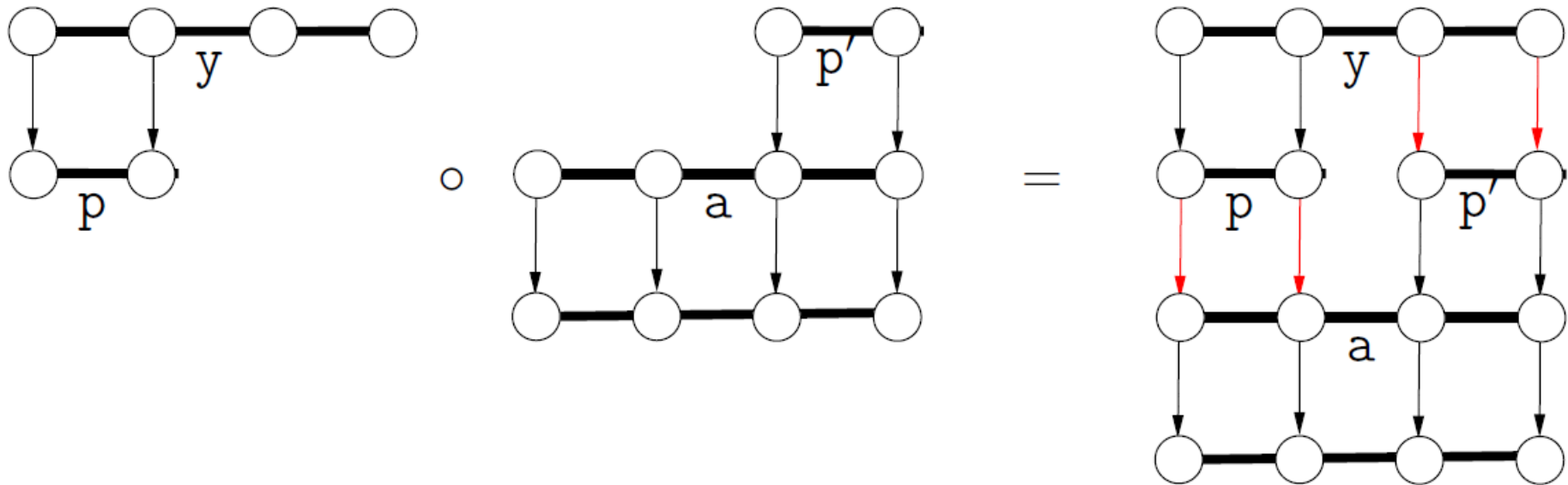
Semantics of negotiations: Mazurkiewicz traces



Semantics of negotiations: Mazurkiewicz traces



Mazurciewicz traces with concatenation



Independence of negotiation atoms
(actually outcomes):

disjoint sets of participants

A grammar for negotiation programs

set of agents X

$prog[X] ::= \epsilon$

do $\{[]\} endalt[X]^+ \{[]\} loopalt[X]^*$ **od**

$prog[Y] \circ prog[Z]$

$endalt[X] ::= name[X]:prog[X']$ **end**

$loopalt[X] ::= name[X]:prog[X']$ **loop**

$name[X] ::= element\ of\ \mathcal{R}_X$

$Y \cup Z = X$

concatenation

for each X a
name space

X' is a subset of X

Semantics of negotiation programs

the empty negotiation

$$\llbracket \epsilon \rrbracket = \{ \llbracket \epsilon \rrbracket \}$$

$$\llbracket \mathbf{do} \bigcup_{i=0}^k E_X^i \bigcup_{j=1}^m L_X^j \mathbf{od} \rrbracket = \left(\bigcup_{j=1}^m \llbracket L_X^j \rrbracket \right)^* \cdot \left(\bigcup_{i=0}^k \llbracket E_X^i \rrbracket \right)$$

$$\llbracket a : P_{X'} \rrbracket = \{ \llbracket a \rrbracket \} \cdot \llbracket P_{X'} \rrbracket$$

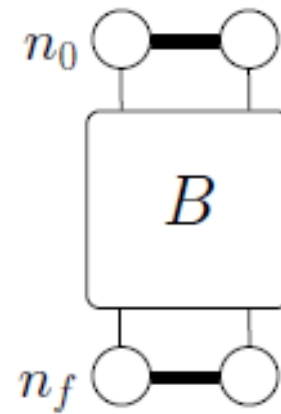
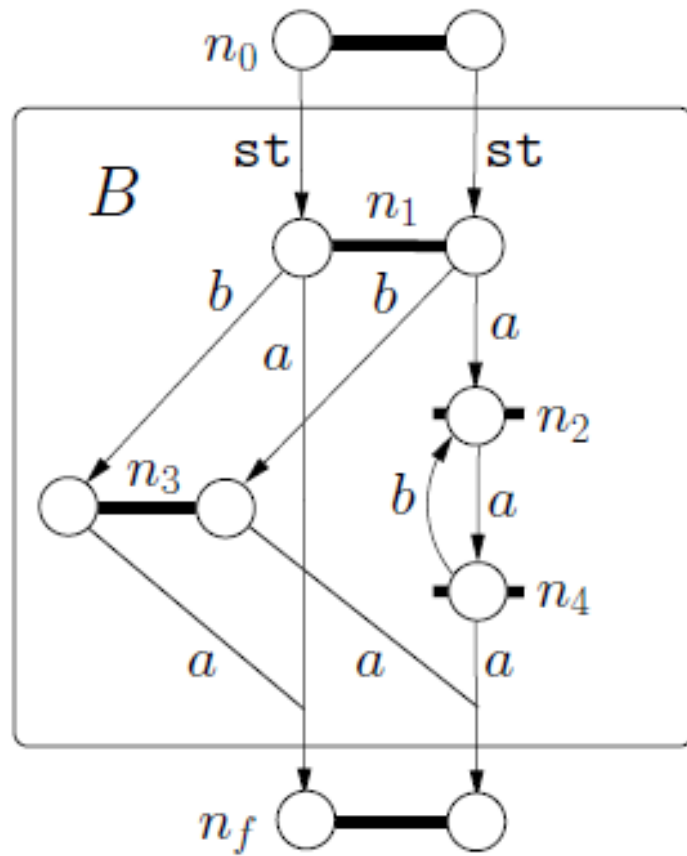
$$\llbracket P_Y \circ P'_Z \rrbracket = \llbracket P_Y \rrbracket \cdot \llbracket P'_Z \rrbracket$$

trace
concatenation

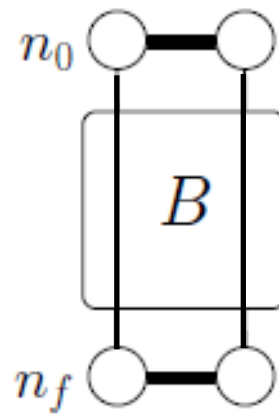
end-
alternative

loop-
alternative

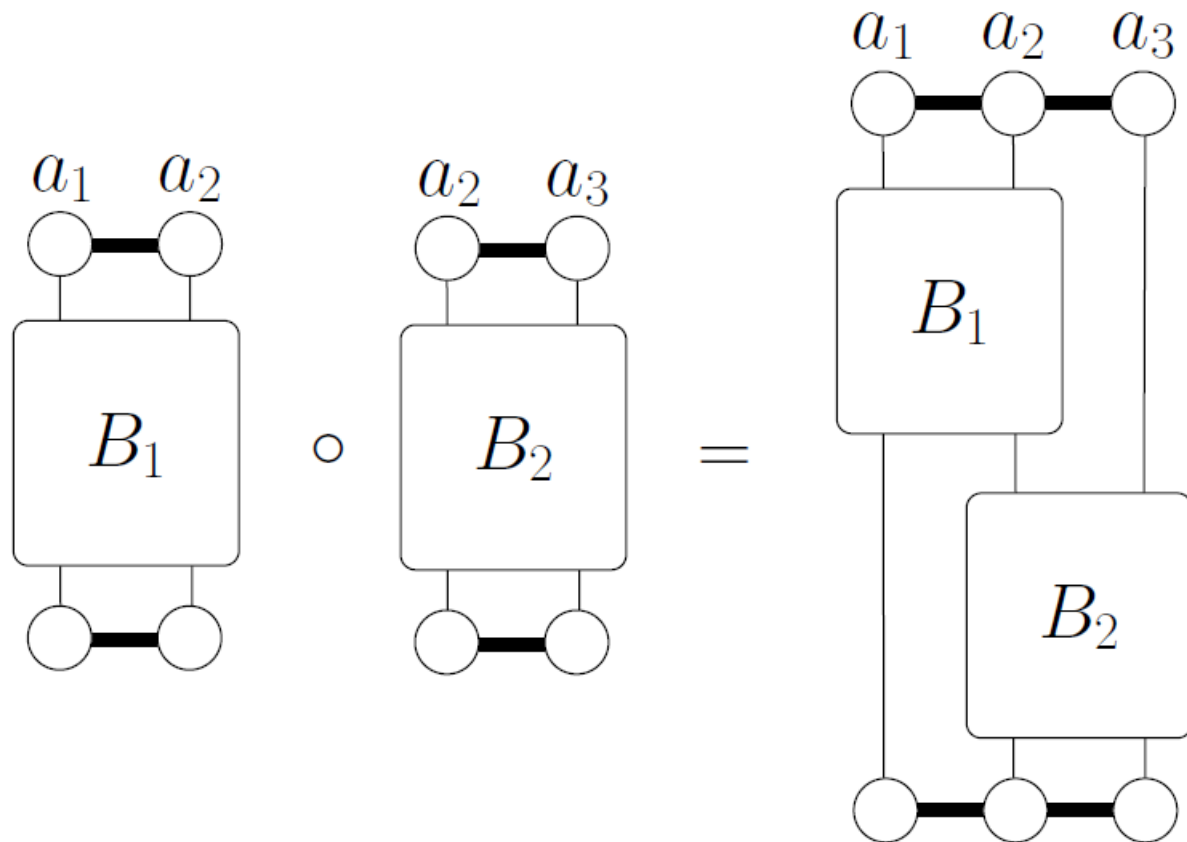
Boxes



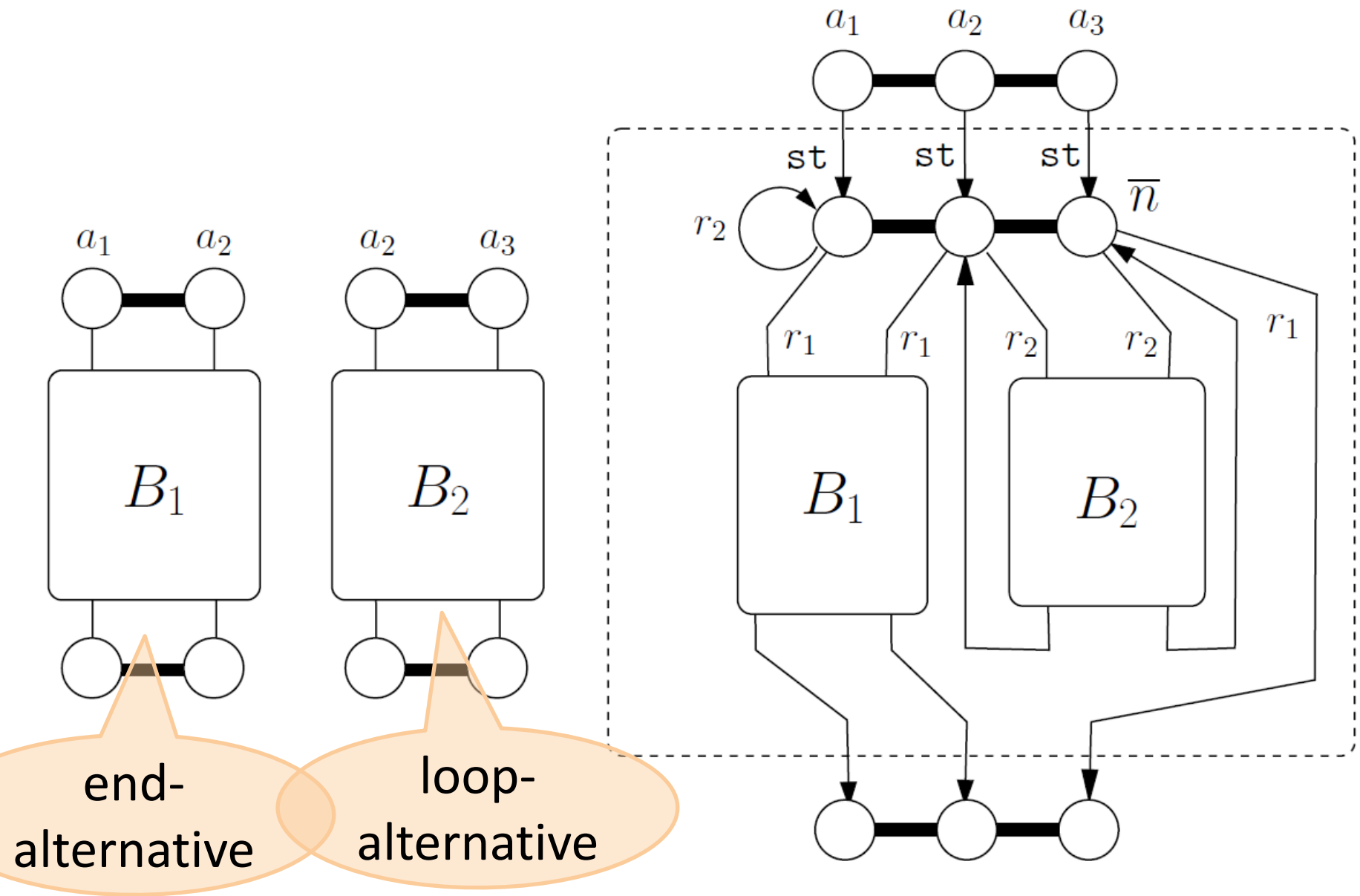
Box for ε



Conatenation of boxes



The alternative operator



Equivalence result

equivalence:
same Mazurciewicz traces

Theorem:

- for each negotiation program there is an equivalent sound and deterministic negotiation which has almost the same size.
- for each sound and deterministic negotiation there is an equivalent negotiation program with the same set of agents.

proof based on reduction results

A concrete programming language

$prog[X] ::= \text{skip}$

$comm[X]$

$\text{do } \{ [] \text{ endgc}[X] \}^+ \{ [] \text{ loopgc}[X] \}^* \text{ od}$

$prog[Y] \circ prog[Z]$

$\text{endgc}[X] ::= \text{guard}[X] : prog[X'] \text{ end}$

$\text{loopgc}[X] ::= \text{guard}[X] : prog[X'] \text{ loop}$

$\text{guard}[X] ::= \text{Guard over the variables of the agents of } X$

$\text{comm}[X] ::= \text{Command over the variables of the agents of } X$

(where neither guards nor commands have to use all variables of the respective sets X of agents).

concrete vs abstract

concrete:

```
agent a  var x = 1: int  
do []  $\neg(x \geq 1)$  : x = x - 1 loop  
    [] (x < 1) : skip end  
od
```

abstract:

```
agent a  
actions a, b, c : {a}  
do []  $\neg a$  : b loop  
    [] c : end  
od
```

a final example

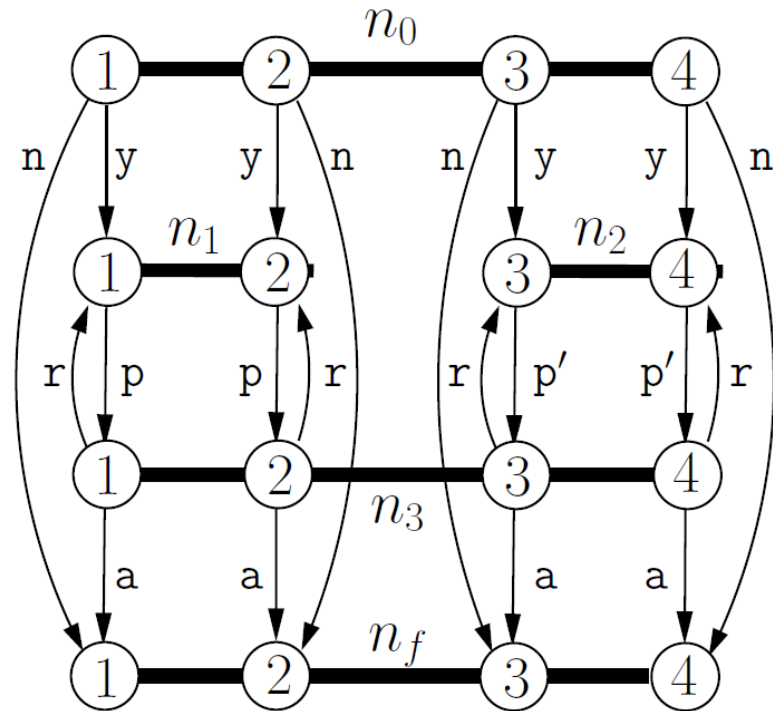
agent a_1 var x_1 :int

...

agent a_4 var x_4 :int

```
1  do []  $\neg(x_1 = x_2 = x_3 = x_4)$  :  
2       $\{x_1, x_2 := f(x_1, x_2) \parallel x_3, x_4 := g(x_3, x_4)\} \circ$   
3      do []  $(x_2 = x_3)$  : end  
4          []  $(x_2 \neq x_3)$  :  
5               $x_2, x_3 = h(x_2, x_3) \circ$   
6               $\{x_1, x_2 := f(x_1, x_2) \parallel x_3, x_4 := g(x_3, x_4)\}$   
7              end  
8          od loop  
9      []  $(x_1 = x_2 = x_3 = x_4)$  : end  
10 od
```

a final example



a final example

agent a_1 var x_1 :int

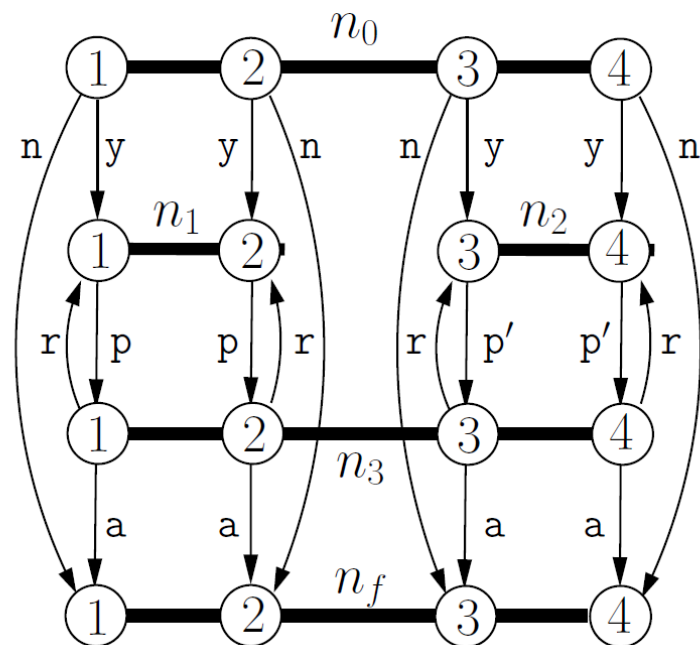
...

agent a_4 var x_4 :int

```

1  do []  $\neg(x_1 = x_2 = x_3 = x_4)$  :
2       $\{x_1, x_2 := f(x_1, x_2) \parallel x_3, x_4 := g(x_3, x_4)\}$ 
3      do []  $(x_2 = x_3)$  : end
4          []  $(x_2 \neq x_3)$  :
5               $x_2, x_3 = h(x_2, x_3) \circ$ 
6               $\{x_1, x_2 := f(x_1, x_2) \parallel x_3, x_4 := g(x_3, x_4)$ 
7              end
8          od loop
9      []  $(x_1 = x_2 = x_3 = x_4)$  : end
10 od

```



On Negotiation as Concurrency Primitive

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